

Fun Sym with Atom Traps

- Parity P symmetry

How to test P symmetry experimentally

Only left-handed ν so far: how do we know?

- \cancel{P} with TRIUMF Neutral Atom trap for β decay
- \cancel{P} in Francium atoms
- How atom traps work
- \cancel{T} experiments *so much time, so little to do*




A. Gorelov

J.A. Behr

J. McNeil 

 M. Ozen

 H. Gallop



D. Melconian



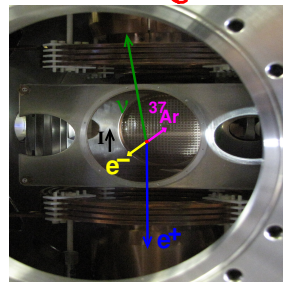
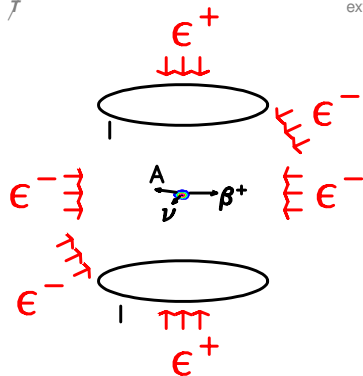
M. Anholm

G. Gwinner

T. Hucko

A. Sharma

L. Xie



Symmetries: Continuous vs Discrete

- Noether's theorem (1915):

Continuous symmetry	→	Conserved quantity
Time-translational invariance	→	Energy
Space-translational invariance	→	Momentum
Rotational invariance	→	Angular momentum
(Laplace-Runge-Lenz vector)	→	name?

THE LATE EMMY NOETHER.

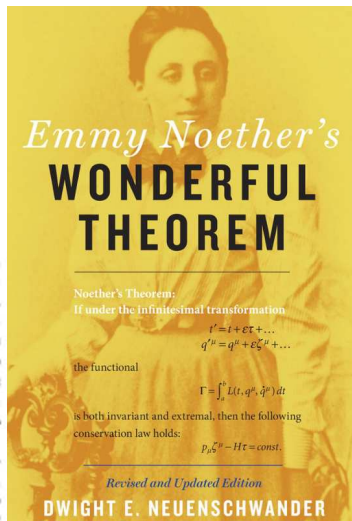
Professor Einstein Writes in Appreciation of a Fellow-Mathematician.

To the Editor of *The New York Times*:

gan. In the realm of algebra, in which the most gifted mathematicians have been busy for centuries, she discovered methods which have proved of enormous importance in the development of the present-day younger generation of mathematicians. Pure mathematics is, in its way, the poetry of logical ideas. One seeks the most general ideas of operation which will bring together in simple, logical and unified form the largest possible circle of formal relationships. In this effort toward logical beauty spiritual formulae are discovered necessary for the deeper penetration into the laws of nature.

In Ted Chiang's "Story of Your Life" aliens think in terms of the action, not position and momentum [Movie "Arrival"]

- Discrete symmetries in quantum mechanics: Parity, Time reversal →



- Wigner considered implications of P , T symmetry conservation in atomic spectra 1926-28. Showed $\langle T\psi_i, T\psi_f \rangle = \langle \psi_f, \psi_i \rangle^*$
 “In quantum theory, invariance principles permit even further reaching conclusions than in classical mechanics.” (D. Gross, Physics Today 48 46 (1995))
- Weyl 1931 considered C , P , T and CPT in “Maxwell-Dirac theory”: $C \Rightarrow$ Dirac eq. negative energy states had to have same mass as the e^- plato.stanford.edu
- From “CP Violation Without Strangeness” Khriplovich and Lamoreaux:
 1949 Dirac “I do not believe there is any need for physical laws to be invariant under reflections in space and time although the exact laws of nature so far known do have this invariance.”

Apr 1956 Asimov “The Dead Past” ν travels backwards in time

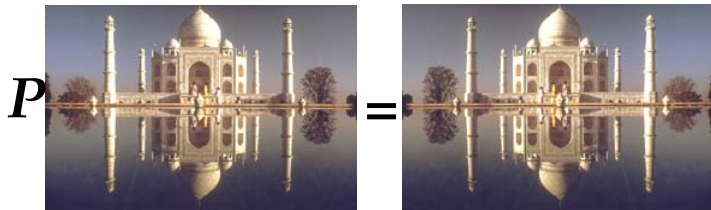
- Oct 1956 Lee and Yang proposed \not{P} in weak decays to fix the θ - τ puzzle
- Feynman gives Ramsey 50:1 odds \not{P} would not be observable
 Ramsey experiment starting at ORNL gets derailed by fission experiments...
 it's OK, Ramsey won 1989 Nobel for his fringes
- 1957 3 simultaneous experimental measurements of $\not{P} \rightarrow$

Parity (From A. Zee “Fearful Symmetry”)

As of 1956, we thought
all interactions
respected parity

Parity operator

$$P \psi(\vec{r}) \rightarrow \pm \psi(-\vec{r})$$

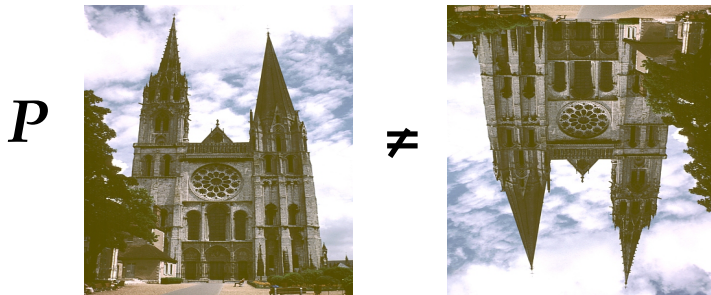


1957:

$\tau - \theta$ Puzzle

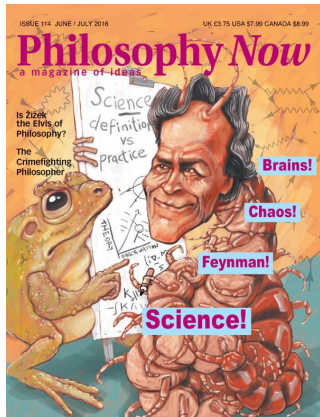
+ μ decay

+ ^{60}Co decay \Rightarrow



Mirrors are not really reversing x,y,z and are kinda confusing

**Plato's
'mirror problem':
"Mirror, Mirror"
T. Wilkinson,
PhilNow 114 (2016)**

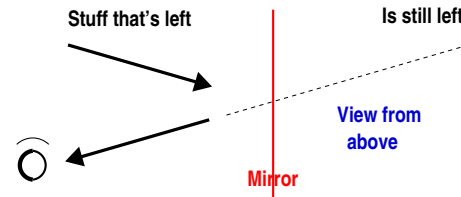
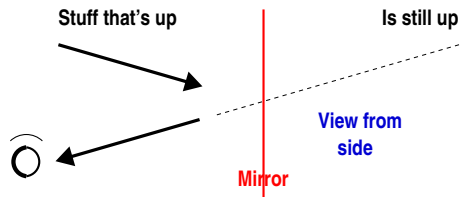


**Plato: Why do mirrors
reverse L-R but not U-D?**
JB: You gotta look at this
diagram. See,
Up stuff stays Up, and
Left stuff stays Left.
Nothing's actually
reversing.

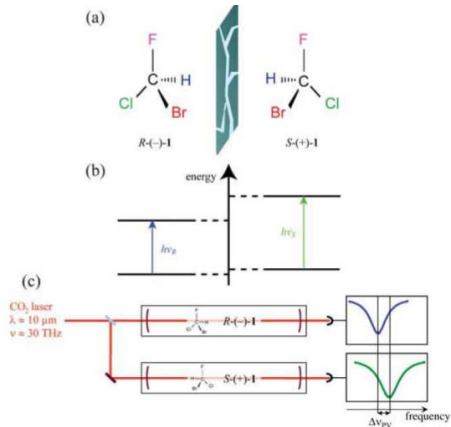
I'd say your interpretation
of 'left' is not quite right 😊

**Plato: 'explains what I'm
missing, but still too
abstract for JB'**

JB thinks Plato and other
philosophy is critical to
humans, but there's not
much deep about mirrors.



Molecule binding energy depends on handedness

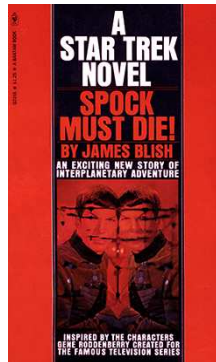


Letokhov, Difference of energy-levels of left and right molecules due to weak interactions. Phys Lett A (1975) 53 275

Darquie et al. CHIRALITY 22 870 (2010) Progress Toward the 1st Observation of \mathcal{P} in Chiral Molecules by High-Resolution Laser Spec

- Very small $\sim 10^{-16}$ to 10^{-14} energy shifts.

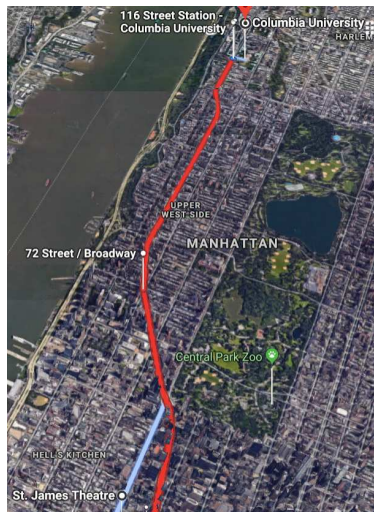
Astrobiology 18 (2018) Selection of Amino Acid Chirality via ν Interactions with ^{14}N in $\vec{E} \times \vec{B}$ Fields
M.A. Famiano, R. N. Boyd...



mirrorSpock
synthesized
wrong-handed
amino acids to
eat

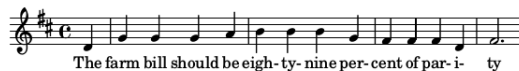
mirrorSpock
was loyal to the
Klingons

Parity: influences? 1956 Broadway Musical Lil' Abner



20 minutes by public transit

Timeless Lyrics: Gene de Paul, music Johnny Mercer



Lee and Yang, theory of parity violation published Oct 1956;
 Opening night Lil' Abner Nov '56 (any free rehearsals?);
 β experiment Wu et al. Jan '57; μ Garwin et al. Jan '57
 (Mom, an admin asst at Columbia, thinks this is unrelated)
 Theory won Nobel; experiment, music did not ☹️

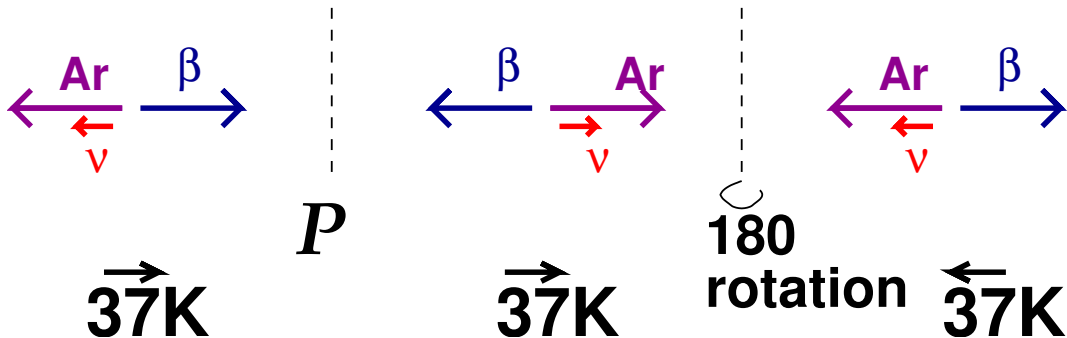
Decays: Parity Operation can be simulated by Spin Flip

Under Parity operation P :

$$\vec{r} \rightarrow -\vec{r}$$

$$\vec{p} \sim \frac{d\vec{r}}{dt} \rightarrow -\vec{p}$$

$$\vec{J} = \vec{r} \times \vec{p} \rightarrow +\vec{J}$$



\Rightarrow A spin flip corresponds exactly to P reversal

Decays don't exactly test T -reversal symmetry



One experimental discovery of parity violation

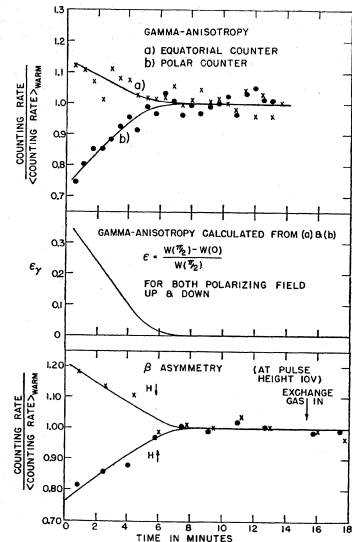
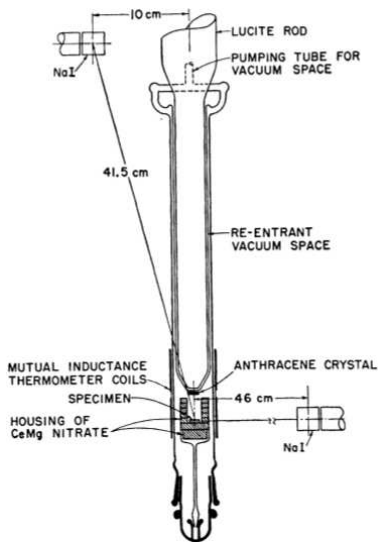


Fig. 2. Gamma anisotropy and beta asymmetry for polarizing field pointing up and pointing down.



**Wu, Ambler, Hayward,
Hopper, Hobson,
PR 105 1413 Feb '57**
**Dilution Refrigerator to
spin-polarize**



$$W[\theta] = 1 + PA\hat{\mathbf{I}} \cdot \frac{\vec{p}_\beta}{E_\beta}$$

$$= 1 + A^V_c \cos[\theta]$$

$$A_{\beta^-} \approx -1.0$$

Followup:

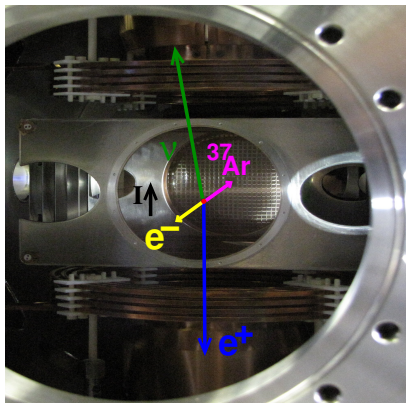


$$A_{\beta^+} > 0$$

CP conserved?

You said you were going to talk about the ν helicity

a different isospin mirror-decay spin-polarized observable

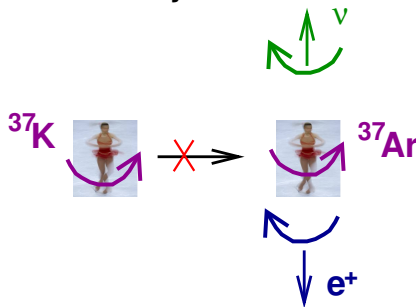


- 10,000 atoms trapped
- P measured in-situ on ^{37}K by atomic method
- ion + shakeoff e^- for A_{recoil}

The neutron community checks this combination of observables for consistency

Mostovoi+Frank Pis'ma Zh. Eksp. Teor. Fiz. 24 45 (1976)

Isobaric mirror decay has helicity-driven null



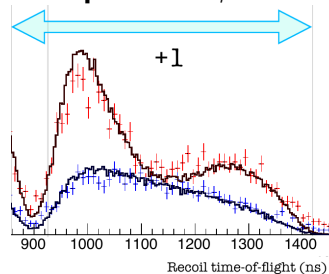
$$W(\theta, P) \approx 1 + a_{\text{pol}} \cos(\theta_{\beta\nu})$$

with $a_{\text{pol}} =$

$$(A_{\beta} - B_{\nu})P - a_{\beta\nu} + 2c/3$$

$= 1$ or 0 , indep of $\frac{M_{GT}}{M_F}$

2014 polarized β -recoil



a_{pol} is an elegant observable, but we may always be statistics-limited— we push upgrades of singles A_{β} and A_{recoil}

UNIVERSITY
OF MANITOBA

FrPNC: Recent results



Claude & Marie-Anne Bouchiat
Used in Cs by Wieman. In Fr:

$$|A_{7s \rightarrow 8s}|^2 = |E1_{\text{Stark}} + E1_{\text{PNC}} + \overset{\text{in PBC}}{M1}|^2$$

$$\approx |E1_{\text{Stark}}|^2 + 2E1_{\text{Stark}}E1_{\text{PNC}}$$

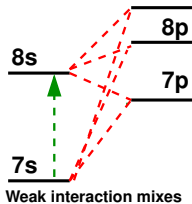
$$E1_{\text{PNC}} \sim 10^{-9} \text{ of an allowed } E1$$

transition amplitude

By picking an E field one can make
the asymmetry $\sim 10^{-3}$

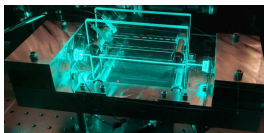
Measurement of $|M1|^2$ with PBC
 $\sim 10^{-13}$ of an allowed $|E1|^2$

T.Hucko, A.Sharma, Kalita, Orozco, Gorelov, Gwinner...

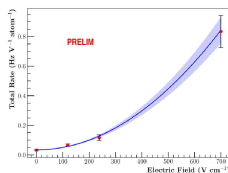
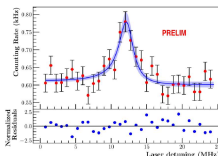


s, p

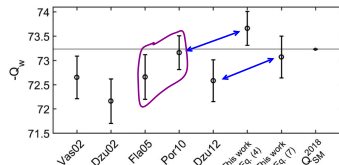
Power buildup cavity
UHV
 $Q \approx 4,000$



T. Hucko, ACOT 2021



Toh Damitz Tanner Johnson Elliott PRL 2019

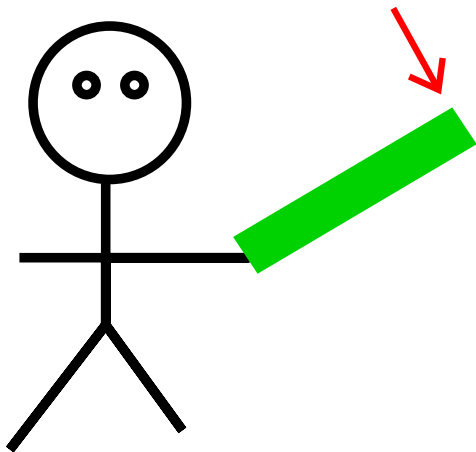


Cs: $E1_{\text{PNC}} \xrightarrow{\text{theory}} Q_W$ disagrees $\sim 1.5 \sigma$
Cs: Asym $\rightarrow E1_{\text{PNC}}$ using measured $M1/\beta$
differs from using other observables

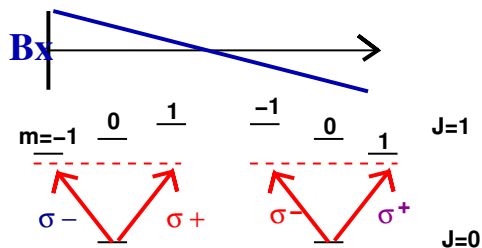
- 8% accuracy differentiates between calculations (theory - exp. $\sim 10\%$ in Cs, only other M1 measured)
- Interference (without PBC) will measure $M1/\beta$ better (Goal 2022)
 $M1 \text{ Fr/Cs} \approx 3$,
so goal is $M1/\beta$ to deterministic accuracy

“Light sabers would make atom traps easy” (H. Norton)

$$\vec{\nabla} \cdot \vec{S} \neq 0$$



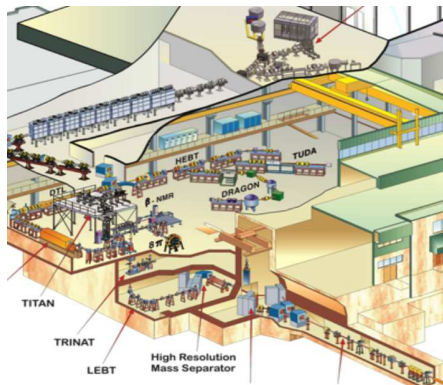
But light sabers violate Poynting's theorem



— **Trapped in MOT** ☐ **Radioactives trapped**
 ○ **Long-lived Rad.** ☐ **Plans**



TRiumf Neutral Atom trap at ISAC

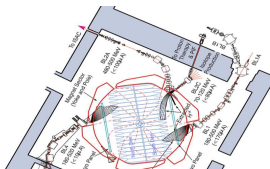


^{37}K $8 \times 10^7/\text{s}$

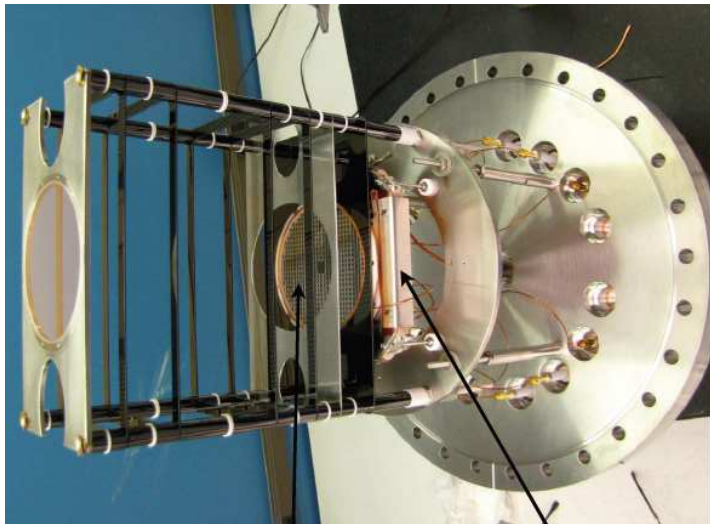
TiC target
 1750°C

$70 \mu\text{A}$
protons

main TRIUMF cyclotron
'world's largest'
 500 MeV H^- (0.5 Tesla)



ion MCP assembly



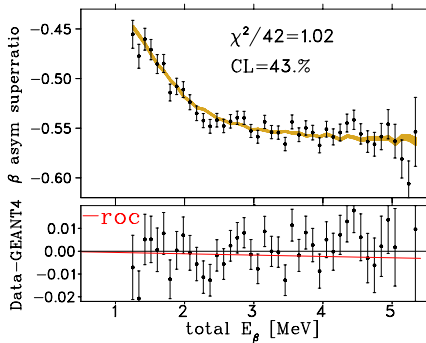
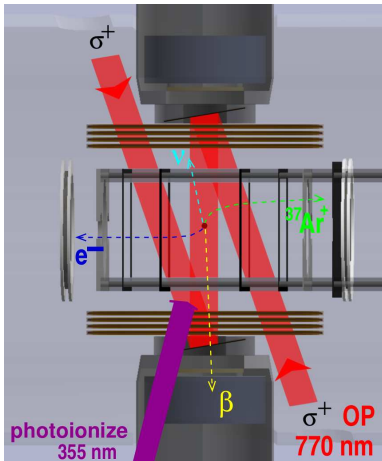
14 inch CF flange

Electrostatic field

**delay-line anode for
position info**

no stray wires

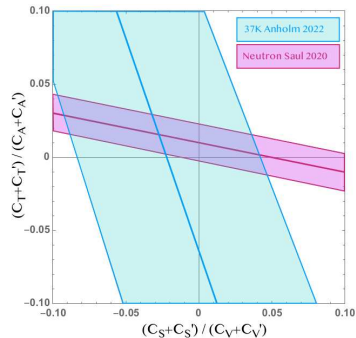
**Low-Z (glassy carbon,
titanium) to minimize β^+
scattering**



Fenker et al. Phys Rev Lett
 120, 062502 (2018)

$A_\beta[\text{experiment}] =$
 -0.5707 ± 0.0019

$A_\beta[\text{theory}] =$
 -0.5706 ± 0.0007



$A_\beta[E_\beta]$ also constrains
 new physics

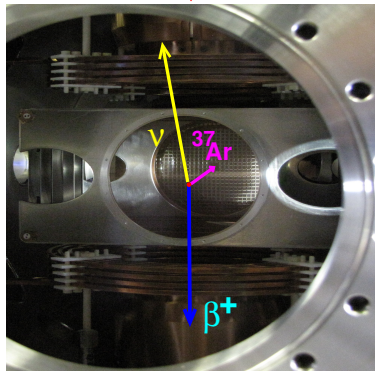
Anholm thesis 2022

$b_{\text{Fierz}} = 0.033 \pm 0.084(\text{stat})$
 $\pm 0.039(\text{syst})$

TRIUMF \mathcal{T} correlation of 3 of 4 momenta

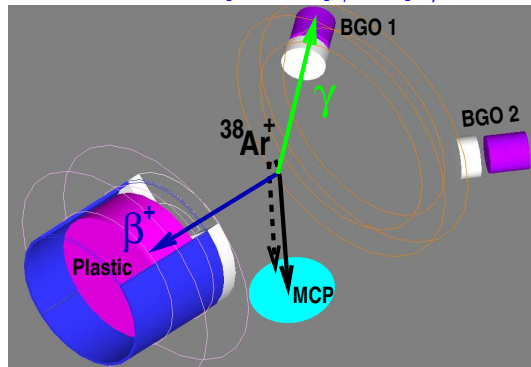
$$\mathbf{t} \rightarrow -\mathbf{t} \Rightarrow \vec{\mathbf{p}} \propto \frac{d\vec{\mathbf{r}}}{dt} \rightarrow -\vec{\mathbf{p}}$$

$$\text{but } \vec{\mathbf{p}}_{\text{recoil}} \cdot \vec{\mathbf{p}}_{\beta} \times \vec{\mathbf{p}}_{\nu} \equiv 0 \quad \text{☹}$$



$$\vec{\mathbf{p}}_{\nu} \cdot \vec{\mathbf{p}}_{\beta} \times \vec{\mathbf{p}}_{\gamma} = -\vec{\mathbf{p}}_{\text{recoil}} \cdot \vec{\mathbf{p}}_{\beta} \times \vec{\mathbf{p}}_{\gamma}$$

$$\xrightarrow{\mathbf{t} \rightarrow -\mathbf{t}} \vec{\mathbf{p}}_{\text{recoil}} \cdot \vec{\mathbf{p}}_{\beta} \times \vec{\mathbf{p}}_{\gamma}$$



- We can test symmetry of apparatus with coincident pairs ☺
- Not exact. Outgoing particles interact → fake \mathcal{T}

EDM in a fundamental particle breaks T : this is exact

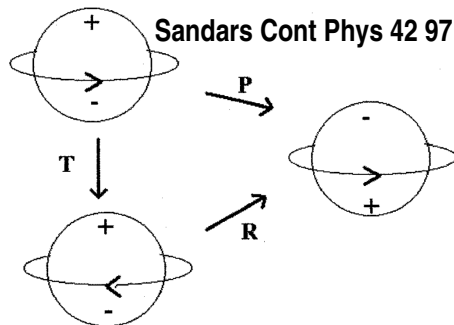
Landau, Nucl. Phys. 3 (1957) p. 127

Electric Dipole moment $\vec{d} = \sum q_i \vec{r}_i$

Since the angular momentum is the only vector in the problem, $\vec{d} = a\vec{J}$

Under T , $\vec{J} \xrightarrow{T} -\vec{J}$ $\vec{d} \xrightarrow{T} +\vec{d}$

If the physics is invariant under T ,
this is a contradiction, $\Rightarrow a = 0$



• The other logical possibility: there are 2 states, with opposite sign of the EDM, and T just formally changes one state to the other.

For most fundamental particles, we know there aren't 2 states

Why do we know the electron doesn't have 2 states?

E.g. some polar molecules have a dipole moment listed in tables, which produces degenerate states and does not break T ...]

\mathcal{T} is related to \mathcal{CP} by the “CPT Theorem”

“All local Lorentz invariant
QFT's are invariant under CPT”

Schwinger Phys Rev 82 914
(1951)

Lüders, Pauli, Bell 1954

- Gravity \rightarrow not flat:

K meson experiments Adler
PhysLettB 364 (1995) 239 test

\mathcal{CPT} to within 1000x expected
from quantum gravity

- Strings not ‘local’

Proofs still pursued \rightarrow

Assuming CPT, $\mathcal{CP} \Leftrightarrow \mathcal{T}$ in most physics theories

The matter excess then motivates \mathcal{T} searches

Studies in History and Philosophy of Modern Physics 45 (2014) 46–65



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On the CPT theorem

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ABSTRACT

We provide a careful development and rigorous proof of the CPT theorem within the framework of mainstream (Lagrangian) quantum field theory. This is in contrast to the usual rigorous proofs in purely axiomatic frameworks, and non-rigorous proof-sketches in the mainstream approach. We construct the CPT transformation for a general field directly, without appealing to the enumerative classification of representations, and in a manner that is clearly related to the requirements of our proof. Our approach applies equally in Minkowski spacetimes of any dimension at least three, and is in principle neutral between classical and quantum field theories: the quantum CPT theorem has a natural classical analogue. The key mathematical tool is that of complexification; this tool is central to the existing axiomatic proofs, but plays no overt role in the usual mainstream approaches to CPT.

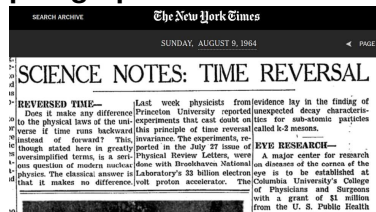
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T , CP , and everything

CP discovery in $K\bar{K}$ got a paragraph in NY Times



'It's never been tested... a theoretical relationship between time and antimatter' Spock, 1966
Sending the Enterprise back in time 3 days must have needed CP well beyond Standard Model 😊

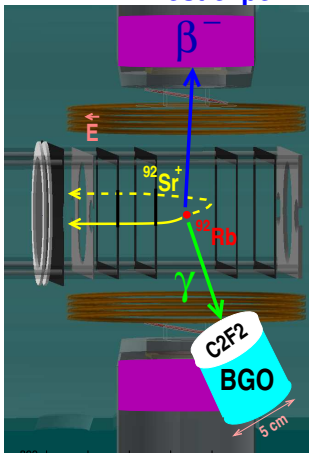
Sakharov immediately laid out ways to use CP at early times to generate the excess of matter observed in the universe ("everything"), but the known amount makes about a billion times less matter than we see

Evidence for CP in accelerator ν 's may make more T2K Nature 580 339 (2020)

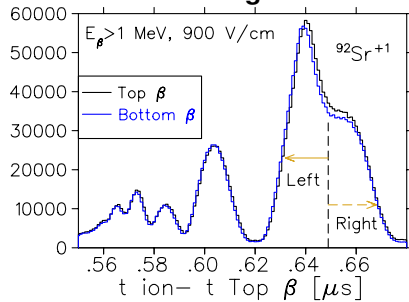
CPT can also do it (Dolgov Phys Rep 222 309 (1992) also mentions Dine-Affleck topological defects)



Test experiment in $^{92}\text{Rb } 0^- \rightarrow 0^+$ decay (no vector current) + $\text{BGO} \rightarrow \text{GAGG}$

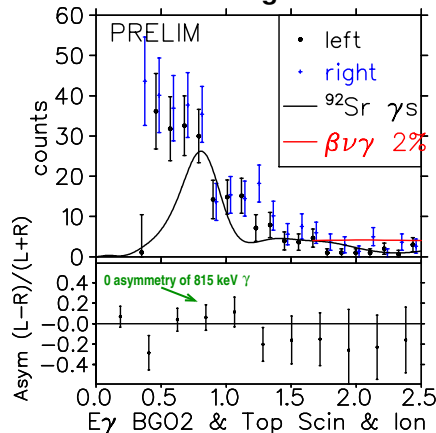


'left' vs. 'right':



(other γ detector sees background from upstream)

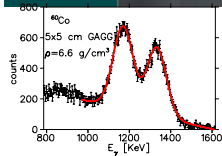
'left' vs. 'right':



$\text{BGO} \rightarrow \text{GAGG} (\text{Ce:Gd}_3\text{Al}_2\text{Ga}_3\text{O}_{12})$

- better E_γ resolution and timing, $\rho = 6.6 \text{ g/cm}^3$
- Good photopeak efficiency (55% at 1 MeV)
- not radioactive like LYSO

Sensitivity to ~ 0.05 to 0.10 asymmetries of few percent branches



Fun Sym with Atom Traps

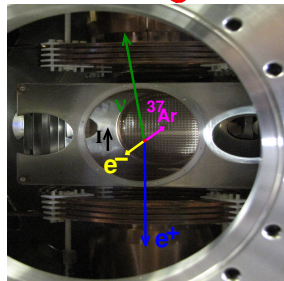
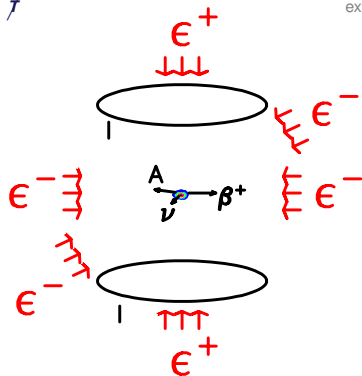
Truth loves its limits, for there it meets the beautiful
Rabindranath Tagore, "Fireflies"

- Parity **P** symmetry

How to test **P** symmetry experimentally

Only left-handed ν so far: how do we know?

- \cancel{P} with TRIUMF Neutral Atom trap for β decay
- \cancel{P} in Francium atoms
- How atom traps work
- \cancel{T} experiments



Preview: Weak interaction breaks parity: Consequences?

'Pulsar kicks'



IGR J11014-6103

$v = 0.01 c$ →

Fuller PRD 2003

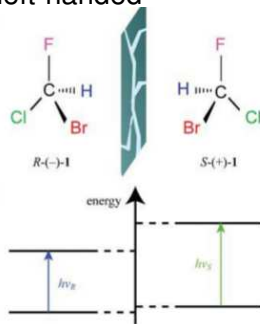
Forced $p + e^- \rightarrow n + \nu$

$$W(\theta) = 1 + \frac{\langle m_I \rangle}{I} \mathbf{A}_\nu \cos(\theta_I)$$

B field polarizes p 's

Need ν_e to include 10^{-8}
admixture of $m_\nu \sim \text{keV}$

Earthling's amino acids are all
left-handed



Letokhov PLA'75

Darquie CHIRALITY 2010

$$\Delta E \sim 10^{14-16} \text{eV}$$

Not Enough for left-handed
bugs to win, so →

Spin-polarized SN ν 's could
preferentially zap
wrong-handed amino acids

Finding the right environment
for spin-polarized amino
acids? e.g. :

Astrobiology 18 (2018)

Selection of Amino Acid

Chirality via ν Interactions

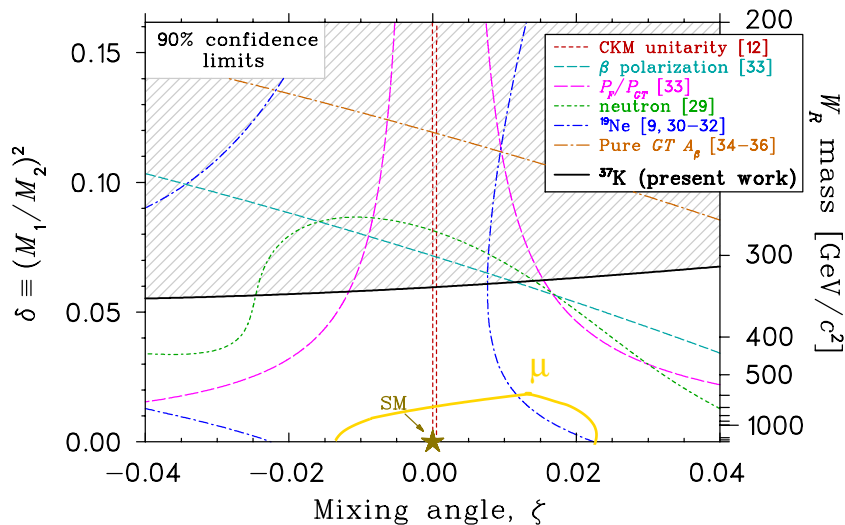
with ^{14}N in $\vec{E} \times \vec{B}$ Fields

M.A. Famiano, R.N. Boyd

(TRIUMF EEC 90's)...



Still no wrong-handed ν 's



Extra W' with heavier mass, couples to wrong-handed ν_R

We can evade TWIST limits by assuming the muon ν_R is heavy
LHC $M'_W > 3.7$ TeV 90%



TRIUMF

The nucleon: a special place for γ 's

Harvey Hill PRL 99 261601 (2007);

EFT with SM interactions combined in the nucleon:
goal was extra γ production by medium-energy ν 's

QCD

Weak

E&M

$$\mathcal{L} = \frac{-4c_5}{m_{\text{nucleon}}^2} \frac{eG_F V_{ud}}{\sqrt{2}} \epsilon^{\sigma\mu\nu\rho} \bar{p} \gamma_\sigma n \bar{\psi}_e L \gamma_\mu \psi_\nu L F_{\nu\rho}$$

Gardner, He PRD 2013: looked for contributions
to radiative n decay. Noticed **QCD antisymmetry**
led to a **scalar triple product of momenta** 😊:

$$|\mathcal{M}_{c5}|^2 \propto \frac{\text{Im}(c_5 g_V)}{M^2} \frac{E_e}{p_e k} (\vec{p}_e \times \vec{k}_\gamma) \cdot \vec{p}_\nu$$

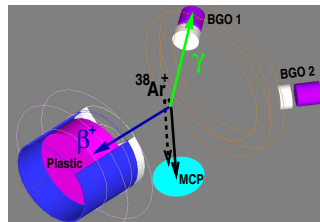
Needs non-SM QCD-like physics,

scale $M \sim 10$'s of MeV

Particles strongly interacting with themselves
but weakly interacting with us

are also possible dark matter candidates

See the 'SIMP miracle' Hochberg et al. arXiv:1402.5143





FrPNC Discovery potential: Weak neutral current

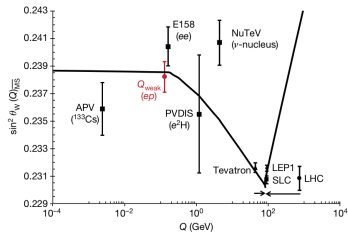


Best prediction of SM: weak neutral current

← Seen 1973 by Gargamelle in ν scattering

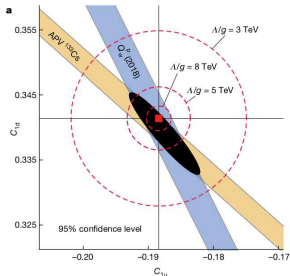
• Could have been 1st measured in ^{18}F γ asymmetry (CSULA, INFN, Mainz, Queens) but isovector/isoscalar $\propto \sin^2(\theta_W)/N_c$

Manitoba @ TRIUMF Fr trap: 10^6 atoms $\Rightarrow < 1\%$ stats in < 1 day



Andronic Nature 2018 (Qweak)

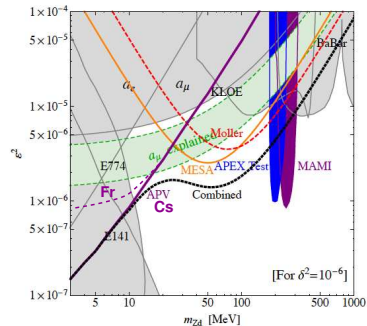
(Recent M_W CDF Science 376 170 2022
would move APV prediction
1 σ down 2204.11991v3)



Sensitivity to new bosons at
mass scale 5 to 8 TeV

• $\text{Fr}/\text{Cs} \propto (\text{rel})Z^2/N \approx 20$
FrPNC goal: exceed Cs

lower-mass Z' Davoudiasl PRL 109 031802 2012



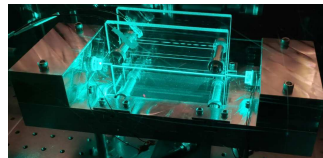
$q_{\text{Cs}} = 2.4 \text{ MeV/c}$, $q_{\text{Fr}} = 10 \text{ MeV/c} \Rightarrow$
different sensitivity to $m_{Z'}$, $\sim \text{MeV}$

An example of university-driven precision measurement, backed by NSERC using TRIUMF-ISAC unique isotope delivery, patiently producing physics



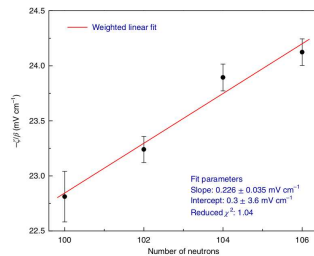
UNIVERSITY
OF MANITOBA

FrPNC: goals and needs



T. Hucko, ACOT 2021

- Atomic parity-violating signal 2024
- Competitive electron-quark neutral weak coupling 2025+
- Nuclear anapole also extracted 2025+ (parity-violating E&M moment induced by nucleon-nucleon weak interaction).
Only measured in ^{133}Cs , $^{205,207}\text{Tl}$: more cases needed
- Needs: Maximum yield and long beamtimes $^{208-213}\text{Fr}$ to beat down systematic uncertainties
- Further needs: $^{220-226}\text{Fr}$ would provide greater lever arm to test SM dependence on N , in competition with Yb $\sim 1\%$ atomic PNC measurements \rightarrow



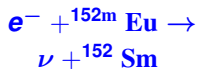
Antypas Budker Nat Phys 15 120 2019

S2139LOI DeMille, Behr, Teigelhöfer would measure Fr_2 dimers in FrPNC trapping facility, to determine s-wave scattering and other properties for high-density Fr.

A full $^{223}\text{FrAg}$ EDM (nuclear $\vec{\tau}$ Schiff moment) exp. needs to laser-cool Ag elsewhere

Measure ν helicity $\epsilon = \hat{s}_\nu \cdot \hat{k}_\nu$ directly: transfer \hat{s}_ν to γ circular polarization; boost \vec{k}_γ by $\pm \vec{k}_\nu$

Goldhaber, Grodzins, Sunyar
Phys Rev 109 1015 (Dec 1957)



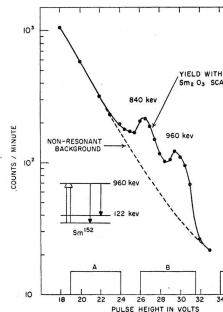
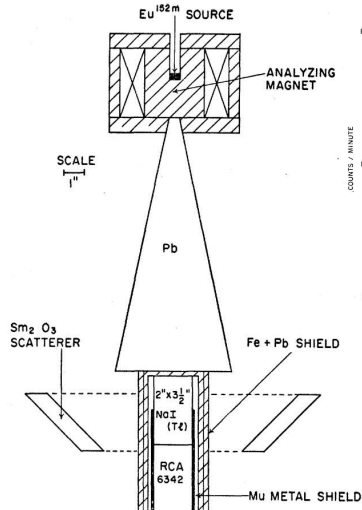
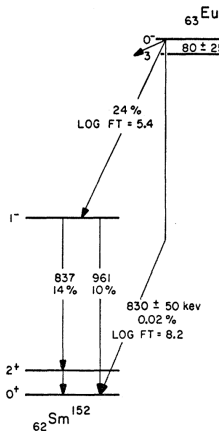
• Upward-going ν populates $\langle I_z \rangle = 0, +1$ **not -1**

• So γ is circularly polarized—transmission through magnet depends on iron polarization:

$$\frac{N_+ - N_-}{N_+ + N_-} = 0.017 \pm 0.003$$

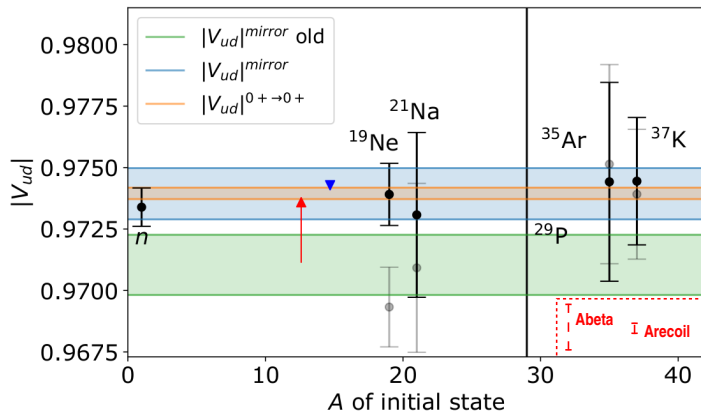
• Upward ν boosts γ momentum so it can be absorbed on-resonance
 $\Rightarrow \nu$ helicity $-1 \pm 10\%$

(• $\bar{\nu}$ helicity $\sim +1$
Palathingal PRL 524 24 '69)



Surprisingly enough, this is the best **direct** measurement of ν helicity $= \hat{s}_\nu \cdot \hat{k}_\nu$

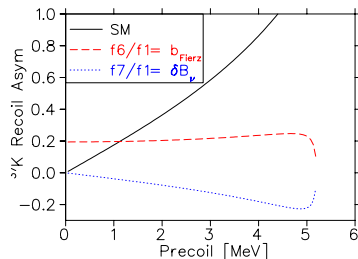
Mirror decays and V_{ud}



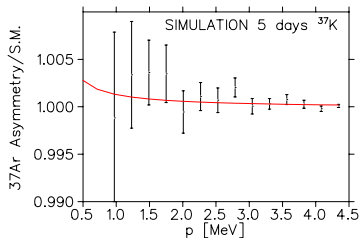
V_{ud} deduced from isobaric mirror decays highlighting the utility of making TRINAT ^{37}K result better
 our projections in red.

L. Hayen and A. Young arXiv 2009.11364

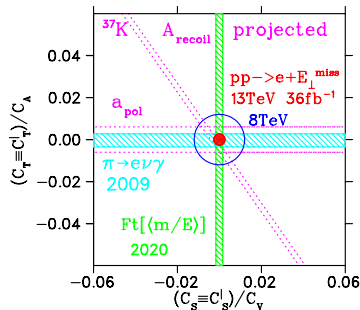
from TRINAT 2023 proposal



The recoil singles asymmetry as a function of recoil momentum from ^{37}K decay, showing the standard model prediction ('SM'), and the functional dependence of the standard model extensions from the Fierz interference term \mathbf{b} ('f6') and changes in ν asymmetry $\delta\mathbf{B}$ ('f7'): this demonstrates the large effects possible from $\delta\mathbf{B}$.



Simulation of 5 days of the ^{37}K recoil singles asymmetry with 10,000 atoms trapped, showing the momentum dependence of the simulated data divided by the standard model prediction.



90% limits from LHC $p + p \rightarrow e^- + E_{\perp}^{\text{miss}} [?]$, $\pi \rightarrow e \nu \gamma [?]$, and $0^+ \rightarrow 0^+$ decay Ft as a function of $E_{\beta} [?]$. Our projected limits from ^{37}K A_{recoil} and a_{pol} (magenta) would provide complementary sensitivity to BSM Lorentz structure.