

# Measure polarization in potassium isotopes

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Dante Prins

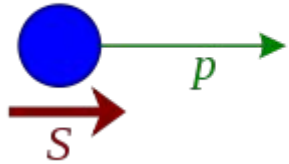


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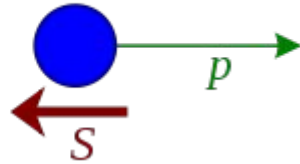
# Potassium 37 beta decay asymmetry experiment

Beta decay is known to violate parity symmetry, having a chirality dependence and a bias for left handedness. Our experiment polarized the parent atom and measures beta emission direction.

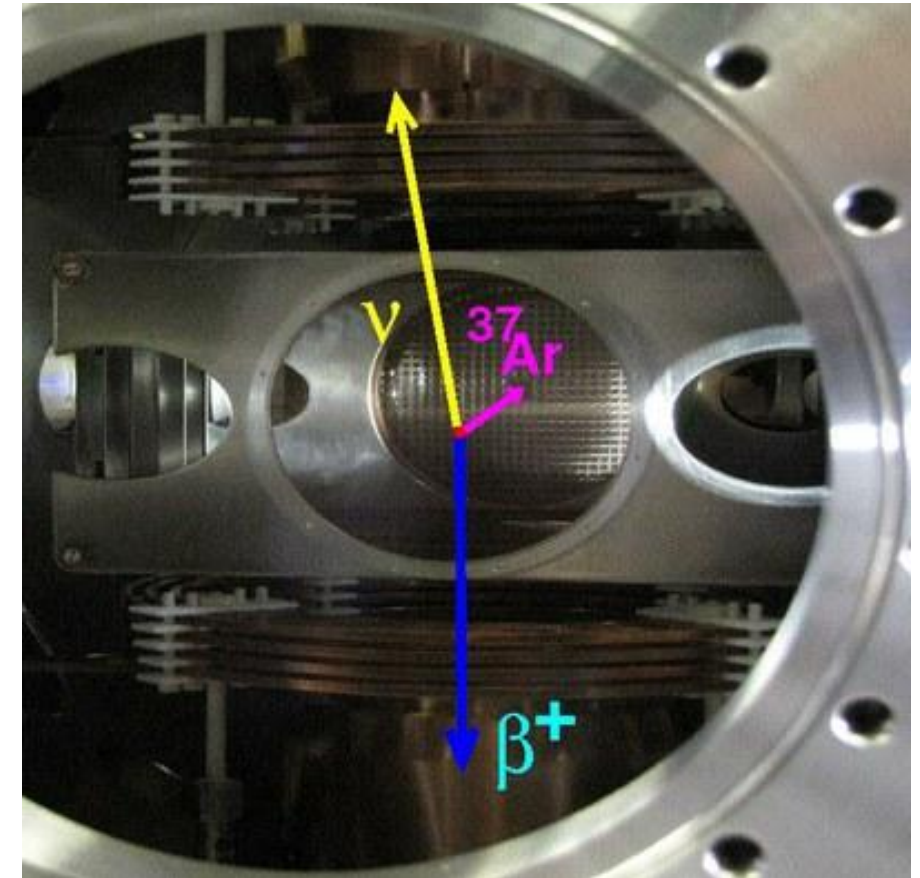
Right-handed:



Left-handed:



$$\mathbf{P} : \begin{pmatrix} x \\ y \\ z \end{pmatrix} \mapsto \begin{pmatrix} -x \\ -y \\ -z \end{pmatrix}.$$

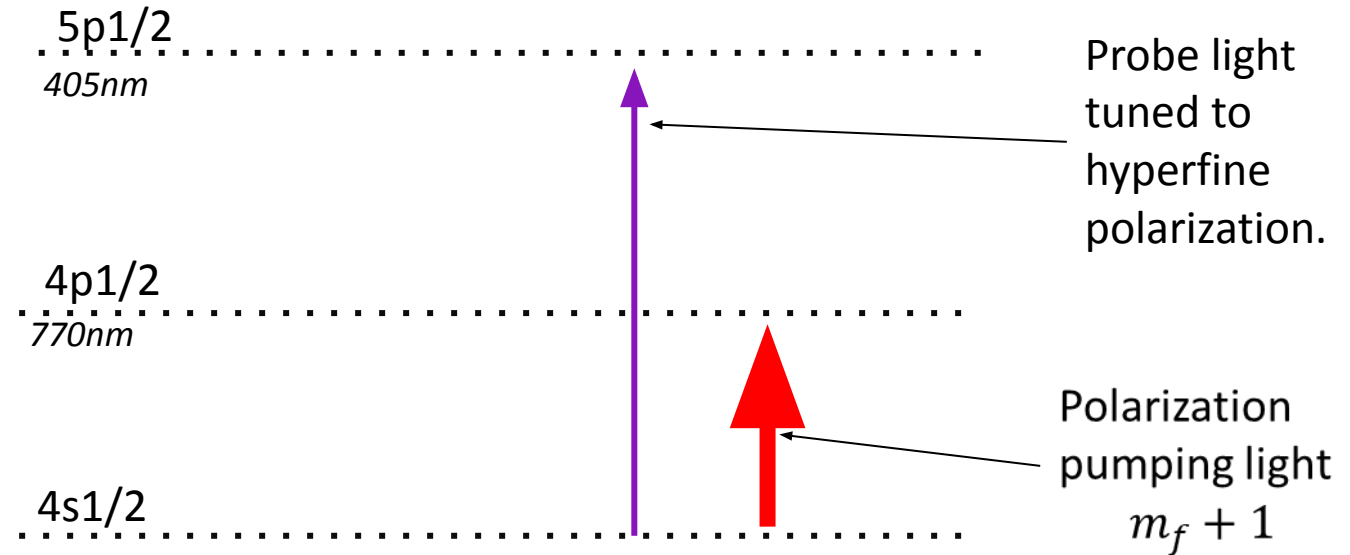
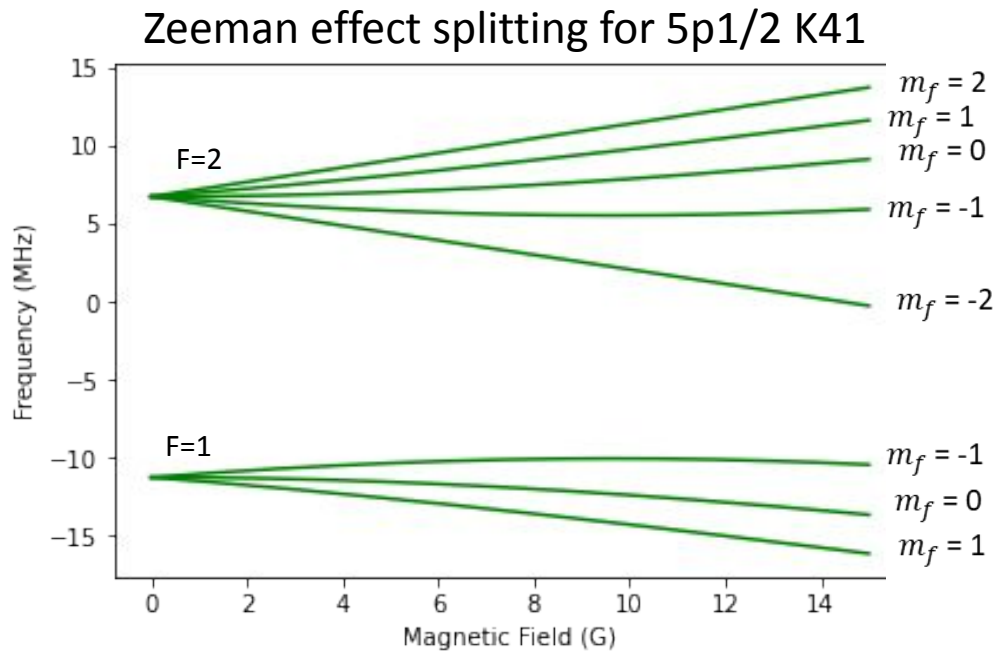


# Polarization measurement

Zeeman effect at medium magnetic fields

$$H = hA I_z J_z + \frac{hA}{2} (J_+ I_- + J_- I_+) + \mu_B B g_J J_z + \mu_N B g_I I_z$$

In the presence of a magnetic field energies will shift allowing us to probe individual polarizations.



$$H = A\vec{I} \cdot \vec{J} - (\mu_N g_I \vec{I} + \mu_B g_J \vec{J}) \cdot \vec{B}$$

Recall the  $|F, m_F\rangle$  basis is conventional for hyperfine states but the Hamiltonian is described in  $|m_I, m_J\rangle$ . For  $J = \frac{1}{2}$ , each hyperfine  $|F, m_F\rangle$  is a linear combination of two states in the  $|m_I, m_J\rangle$  basis, leading to a two state degenerate perturbation problem for each  $|F, m_F\rangle$  state.

Defining the basis as  $|\pm\rangle = |m_J, \pm\frac{1}{2}, m_I = m_F \mp \frac{1}{2}\rangle$ , through ladder operations we get

$$H = \begin{pmatrix} -\frac{A}{4} + \mu_N g_I m_F B + \frac{1}{2}(A m_F + \mu_B g_J - B \mu_N g_I) & \frac{1}{2} A \sqrt{(I + \frac{1}{2})^2 - m_F^2} \\ \frac{1}{2} A \sqrt{(I + \frac{1}{2})^2 - m_F^2} & -\frac{A}{4} + \mu_N g_I m_F B - \frac{1}{2}(A m_F + \mu_B g_J - B \mu_N g_I) \end{pmatrix}$$

The positive eigenenergy is defined as  $F = 2$  while the negative  $F = 1$

$$\Delta E_{F=2} = -\frac{A}{4} + \mu_N g_I m_F B + A \sqrt{1 + m_F x + x^2}$$

$$\Delta E_{F=1} = -\frac{A}{4} + \mu_N g_I m_F B - A \sqrt{1 + m_F x + x^2}$$

$$\text{Where } x = \frac{B(\mu_B g_J - \mu_N g_I)}{2A}.$$

Eigenstates found are then

$$|F = 2, m_F\rangle = \alpha |+\rangle + \beta |-\rangle$$

$$|F = 1, m_F\rangle = \beta |+\rangle + \alpha |-\rangle$$

where

$$\alpha = \frac{1}{2} + \frac{Am_F + B\mu_B g_J - B\mu_N g_I}{4A\sqrt{1+m_F x+x^2}}$$

$$\beta = \frac{1}{2} - \frac{Am_F + B\mu_B g_J - B\mu_N g_I}{4A\sqrt{1+m_F x+x^2}}$$

Notice we recover the Clebsch-Gordan Coefficients at  $B = 0$  and that at  $B \rightarrow \infty$  we reach pure states, namely  $|F = 2, m_F\rangle = |+\rangle$  and  $|F = 1, m_F\rangle = |-\rangle$ .

For  $m_F = \pm 2$ , where the states are already pure at  $B = 0$ , the Hamiltonian reduces to single state solutions where

$$\Delta E_{F=2} = \frac{A^3}{4} + \mu_N g_I m_F B$$

$$\Delta E_{F=1} = -\frac{A^5}{4} + \mu_N g_I m_F B$$

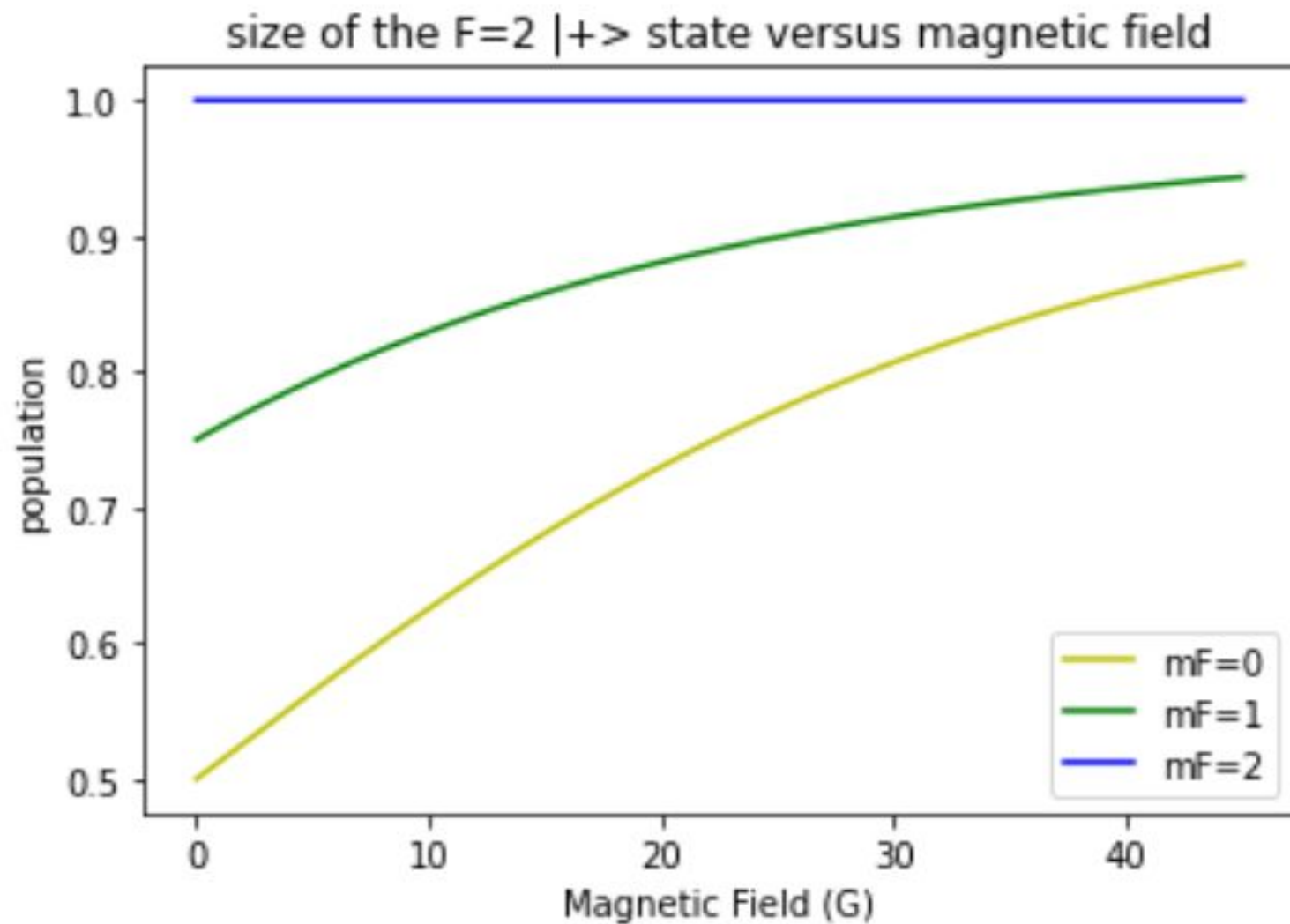
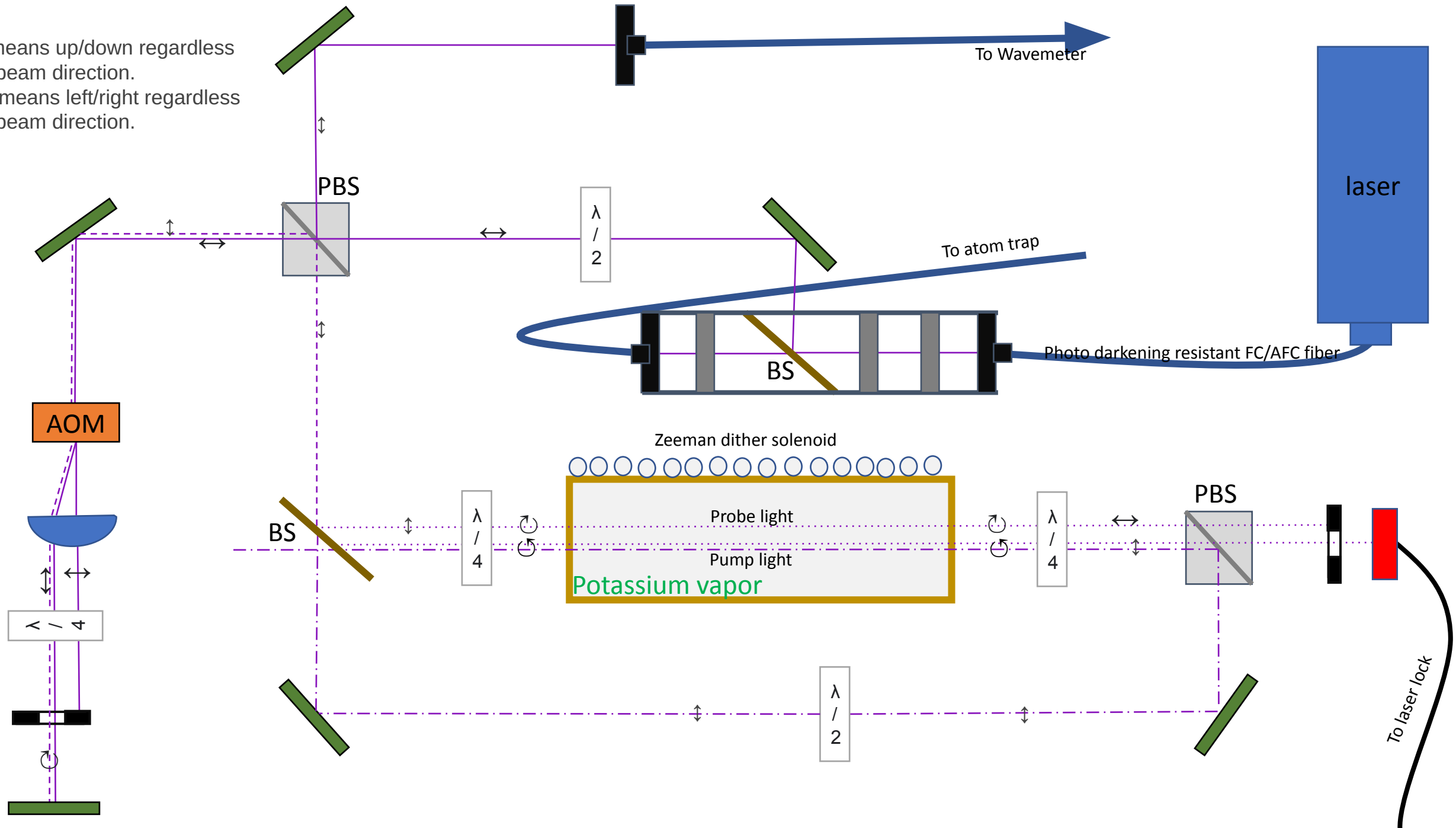


Figure 2: plot of the coefficient  $\alpha$  from  $|F = 2, m_F\rangle = \alpha |+\rangle + \beta |-\rangle$  as a function of magnetic field. Note that  $\beta = 1 - \alpha$ .

$\updownarrow$  means up/down regardless of beam direction.  
 $\leftrightarrow$  means left/right regardless of beam direction.



# Hyperfine structure splitting varies by isotope

Isotope	Abundance
K37	1.23s half life
K39	93%
K41	7%

$$H_{HFS} = A \mathbf{I} \cdot \mathbf{J}$$

$$K37 A_{4s_{1/2}} = 240.3\text{MHz}$$

$$K39 A_{4s_{1/2}} = 461.7\text{MHz}$$

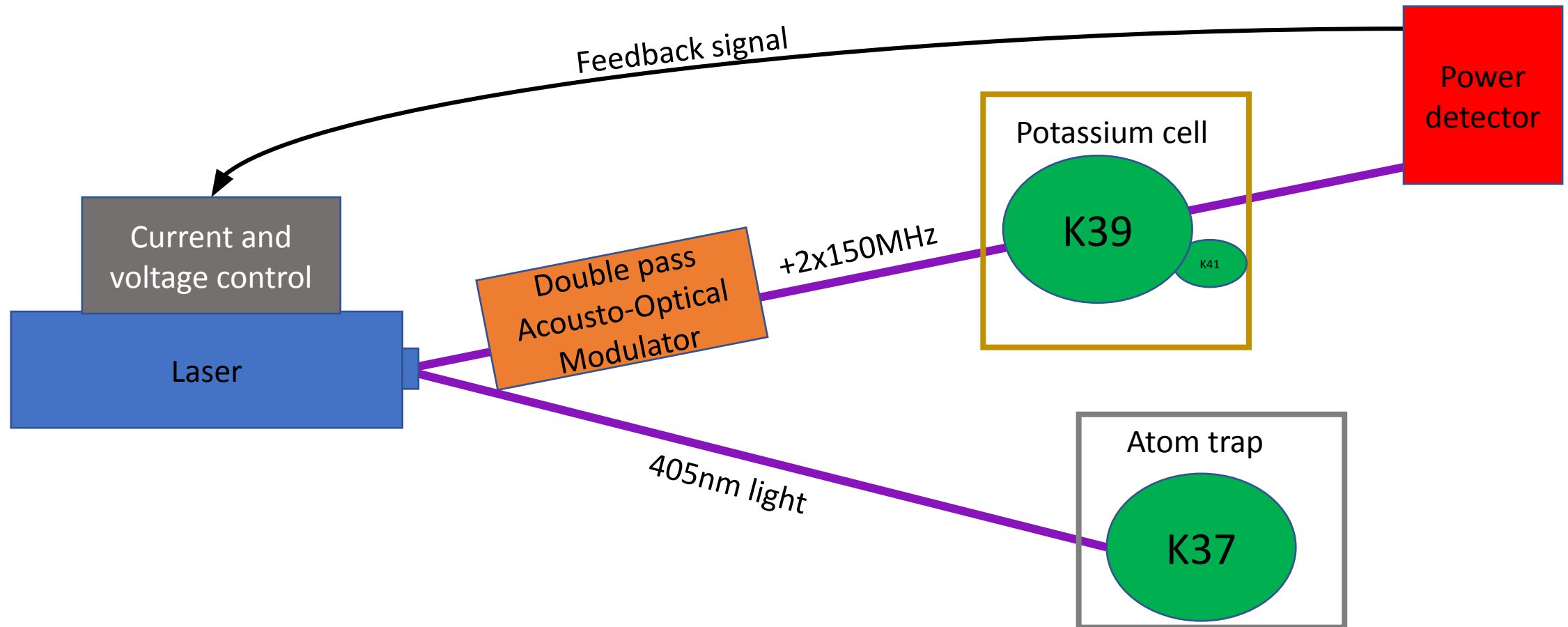
$$K41 A_{4s_{1/2}} = 254.0\text{MHz}$$

How do we lock the trap to K39 spectra but scan K37?

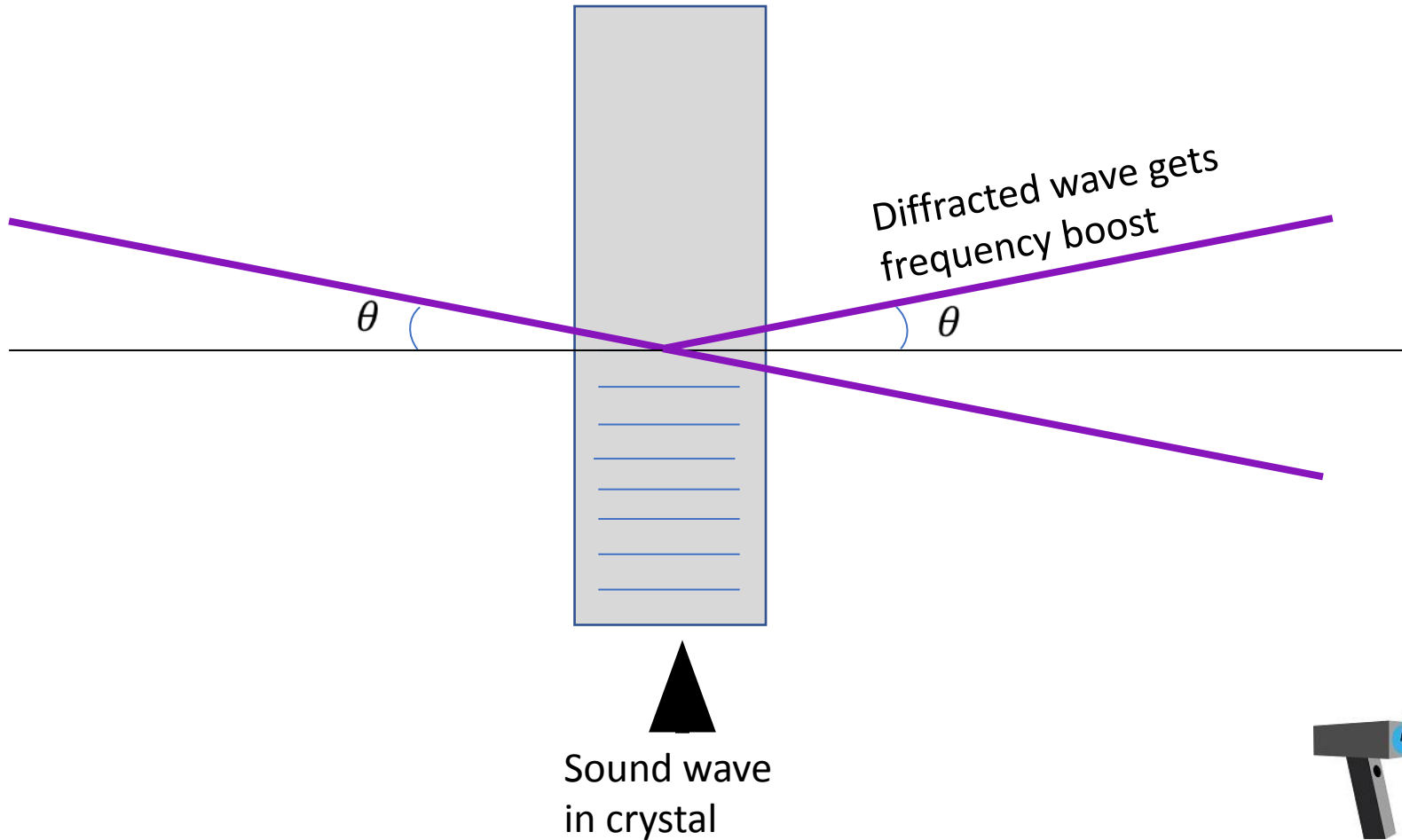


# Isotope frequency shift is corrected by Acousto-Optical Modulator

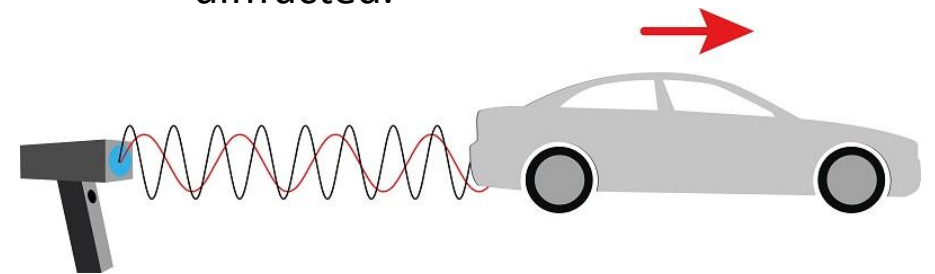
Picture of aom module



# Acousto-Optical Modulator physics

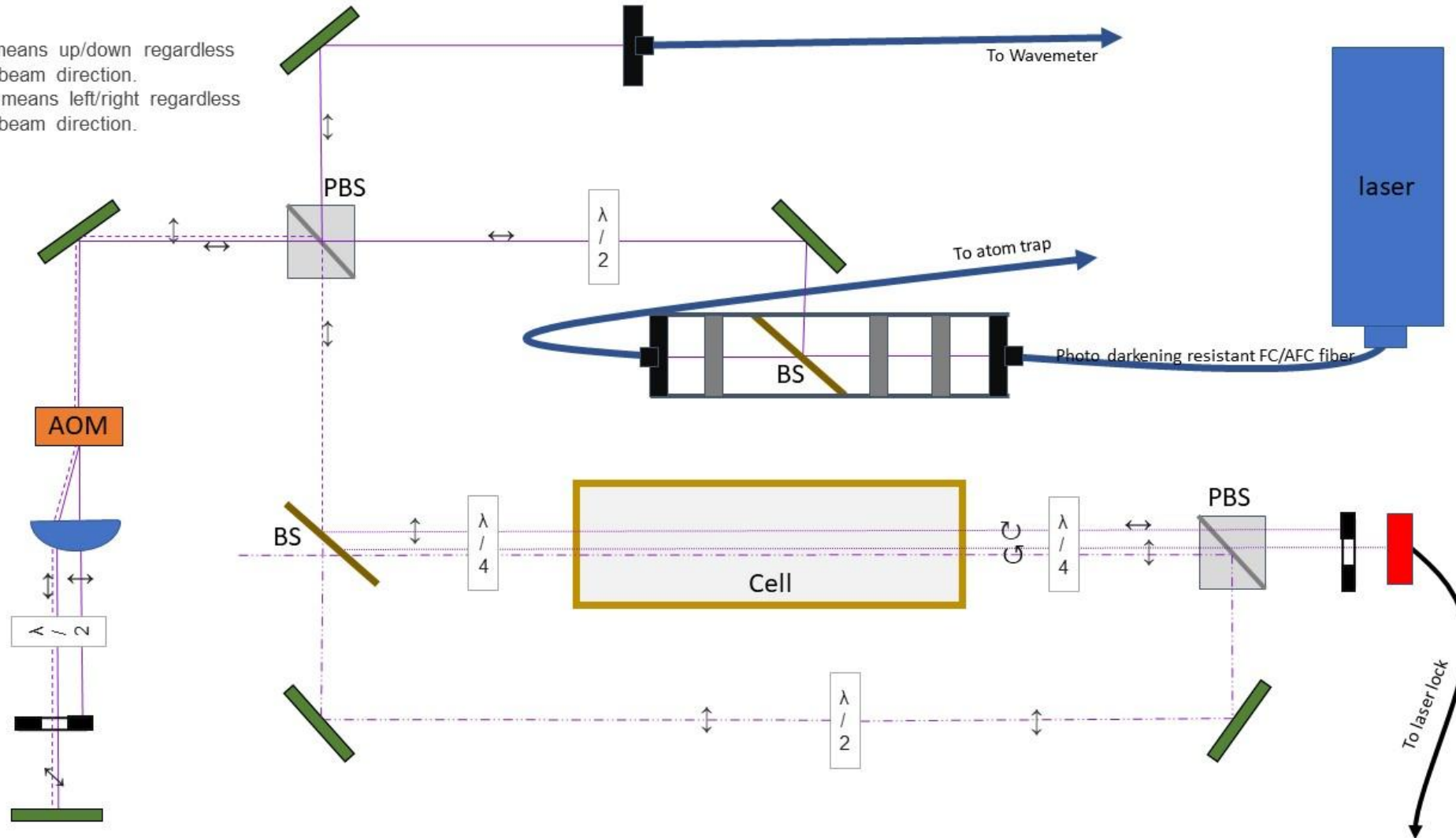


The incoming light is Doppler shifted to a higher frequency in the reference frame of the moving Bragg plane before being diffracted.



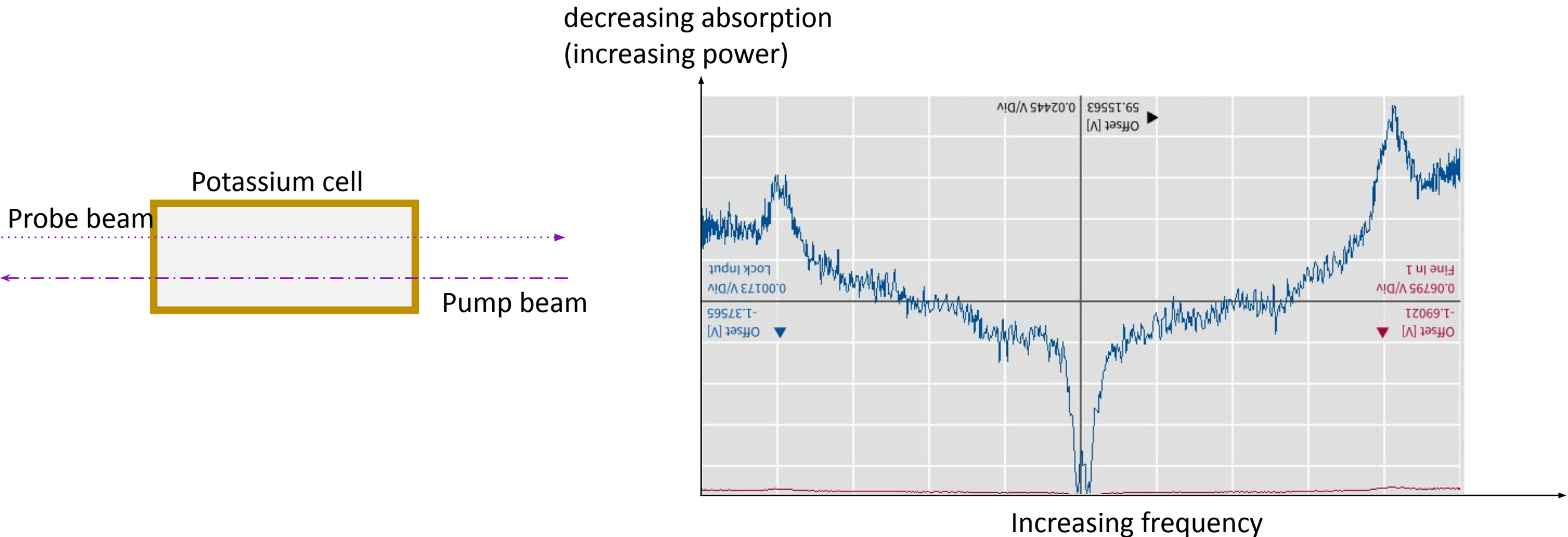
# Beam polarization

↑ means up/down regardless of beam direction.  
↔ means left/right regardless of beam direction.

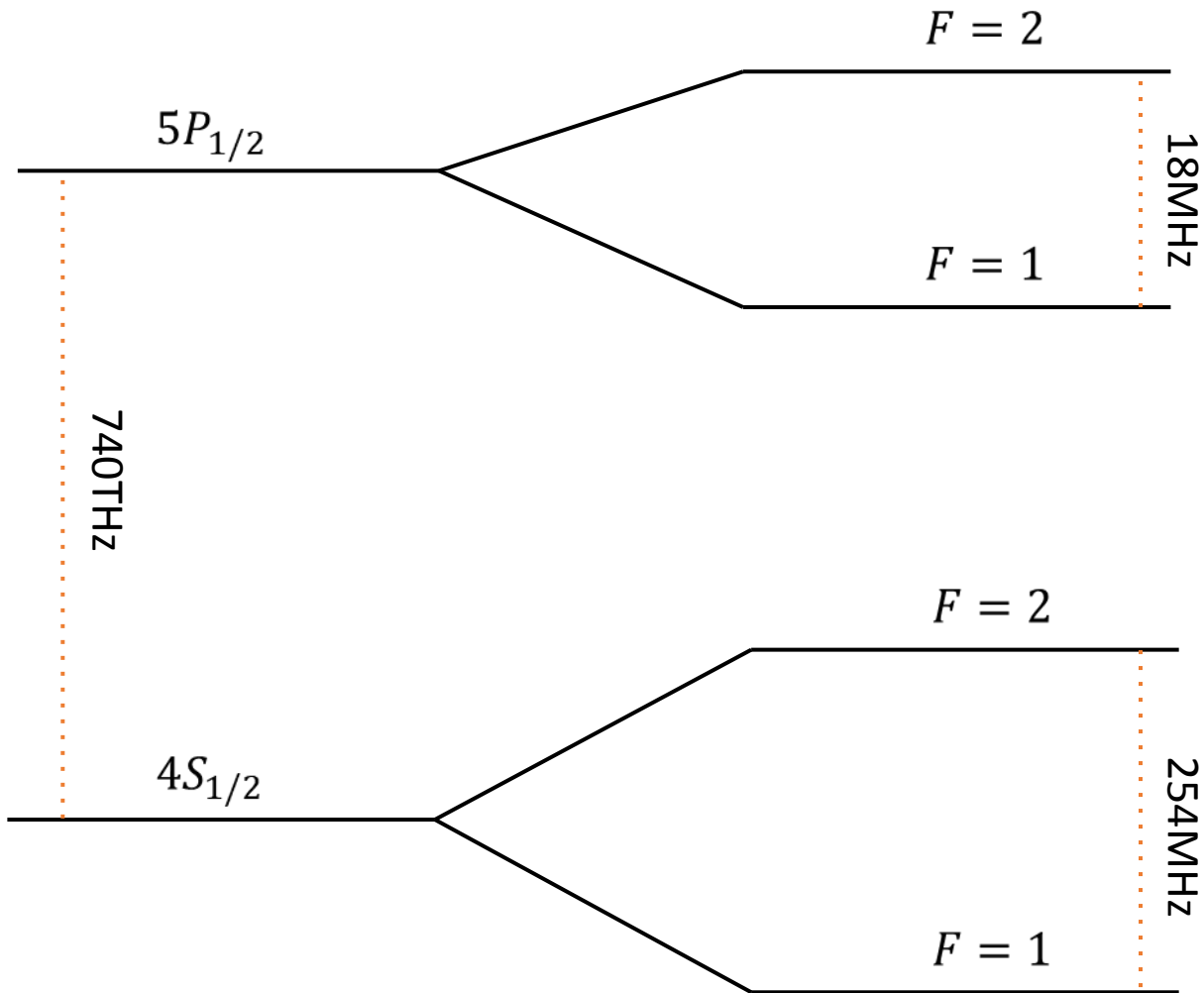


# K cell sat spectroscopy

We know the cell will absorb light at transitions frequencies, how do we arrive at the actual absorption signal?



# Hyperfine structure frequencies for K39



	295MHz
	277MHz
	-166MHz
	-184MHz

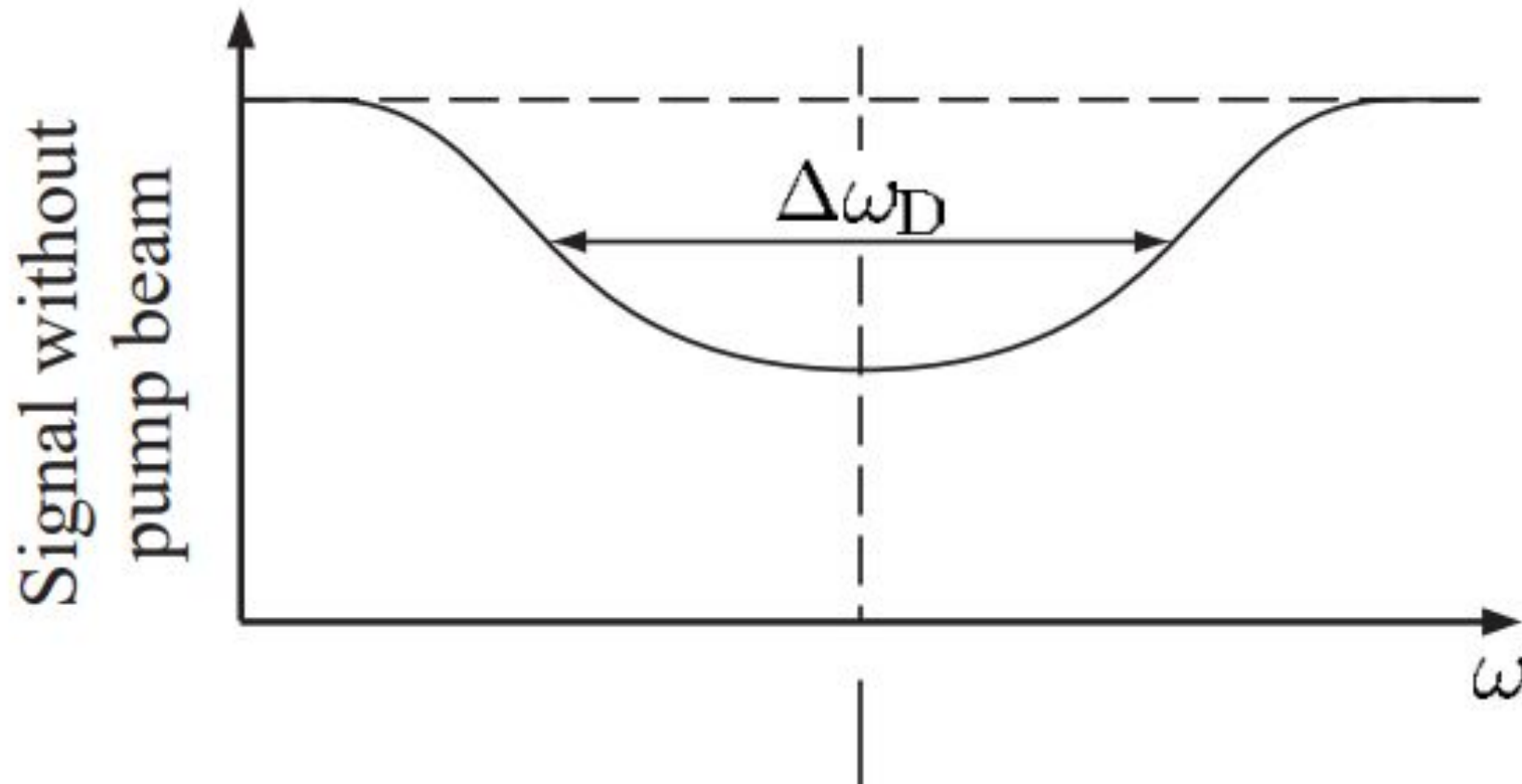
$$H_{HFS} = A \mathbf{I} \cdot \mathbf{J}$$

$$A_{4S_{1/2}} = 126.9\text{MHz}$$

$$A_{5P_{1/2}} = 8.99\text{MHz}$$

# Doppler shift broadened absorption

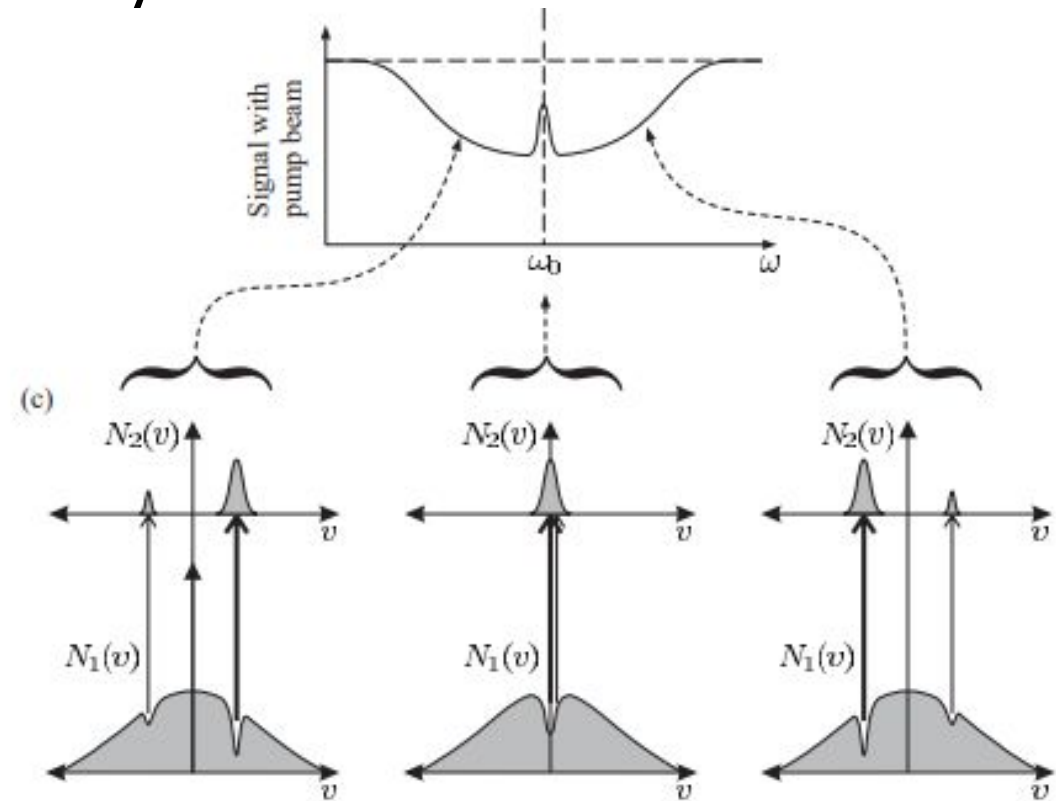
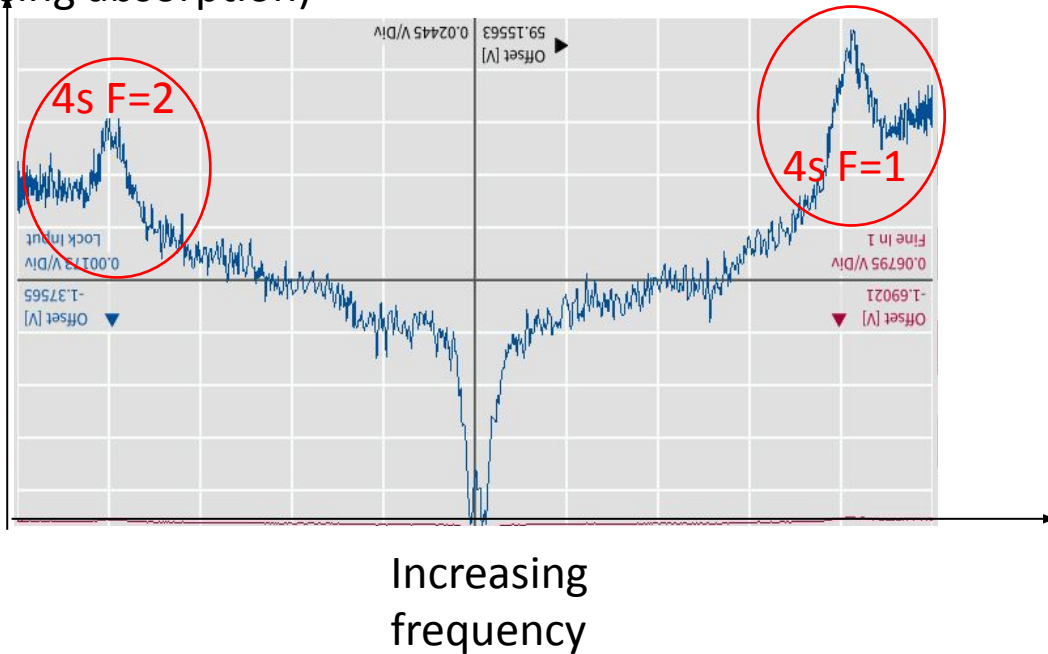
Decreasing absorption  
(increasing power)



# Pump beam hole burning

Now that our absorptions are Doppler smeared, we use the pump beam to select atoms with zero velocity.

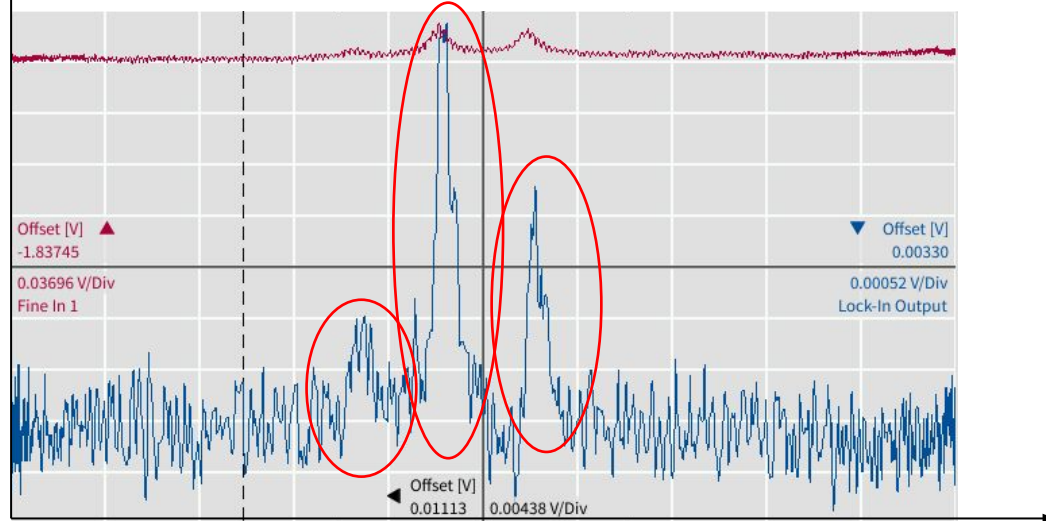
Increasing power  
(decreasing absorption)



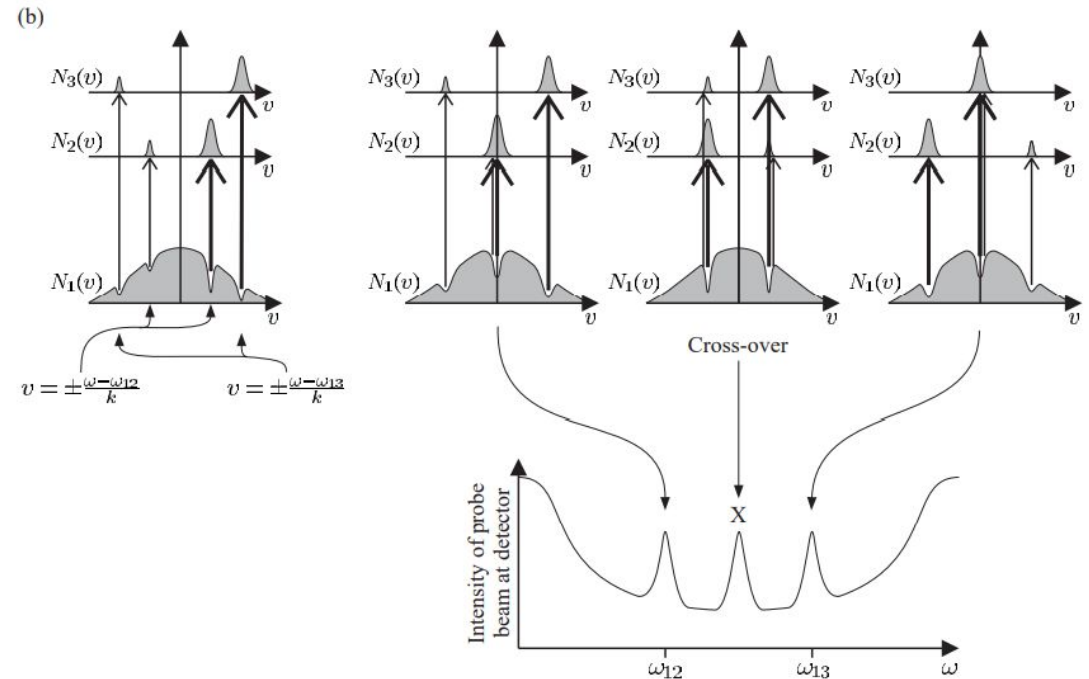
# Crossover effect

Every pair of peaks has a composite peak halfway in between from the doppler shifts of the two side peaks.

Increasing power  
(decreasing absorption)



Increasing  
frequency

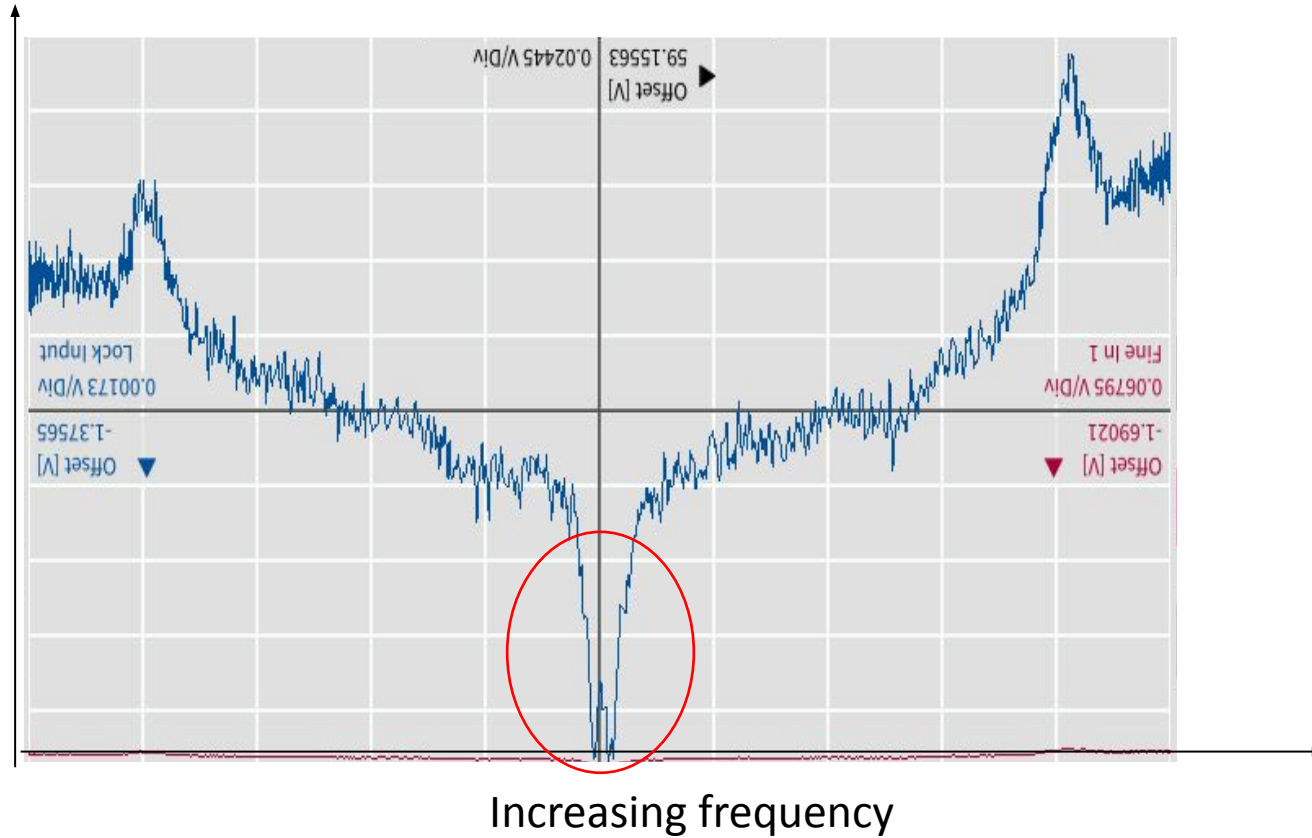


'Atomic Physics' by Foot.



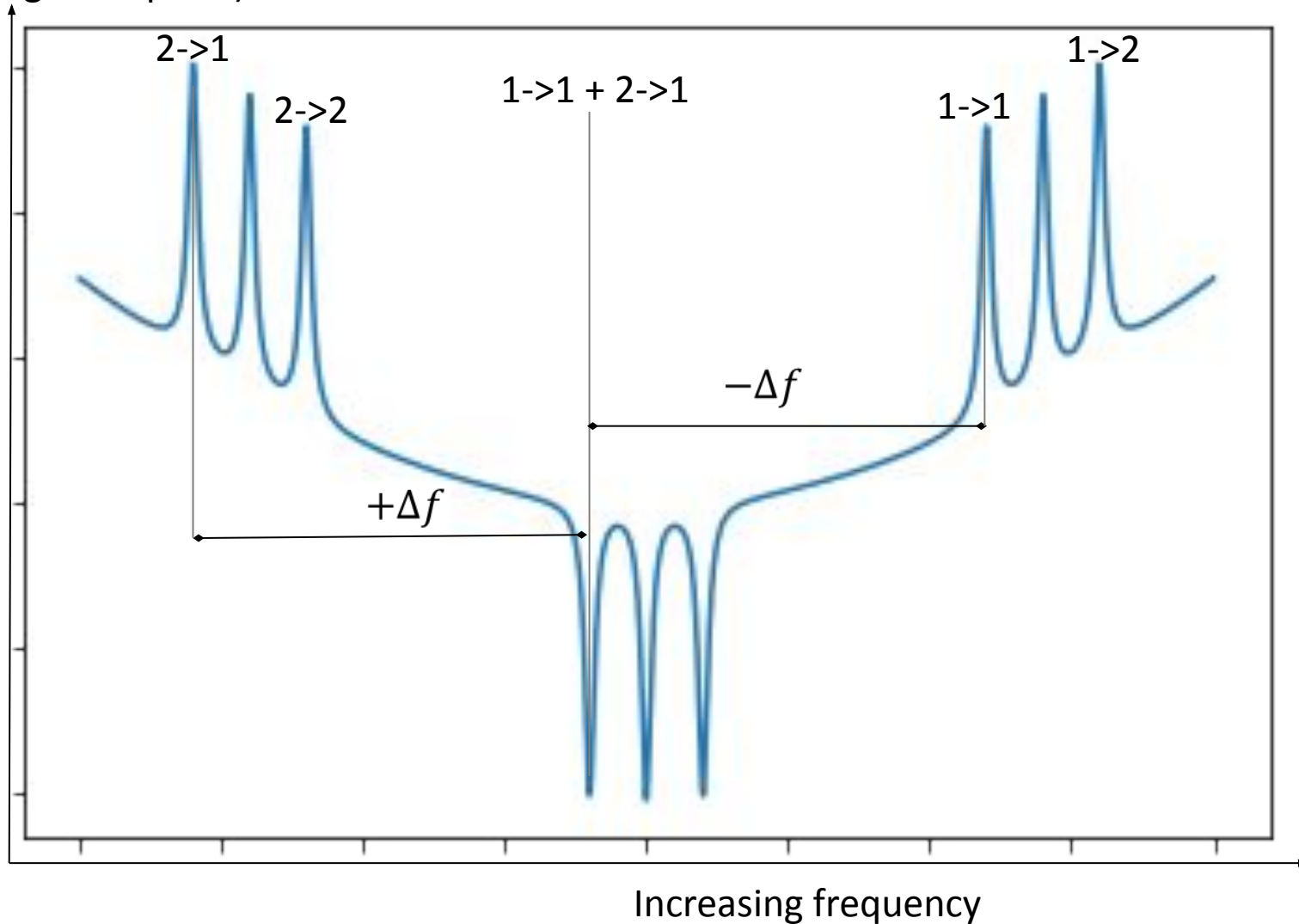
# Enhanced absorption

Increasing power (decreasing absorption)



# Enhanced absorption

Increasing power  
(decreasing absorption)

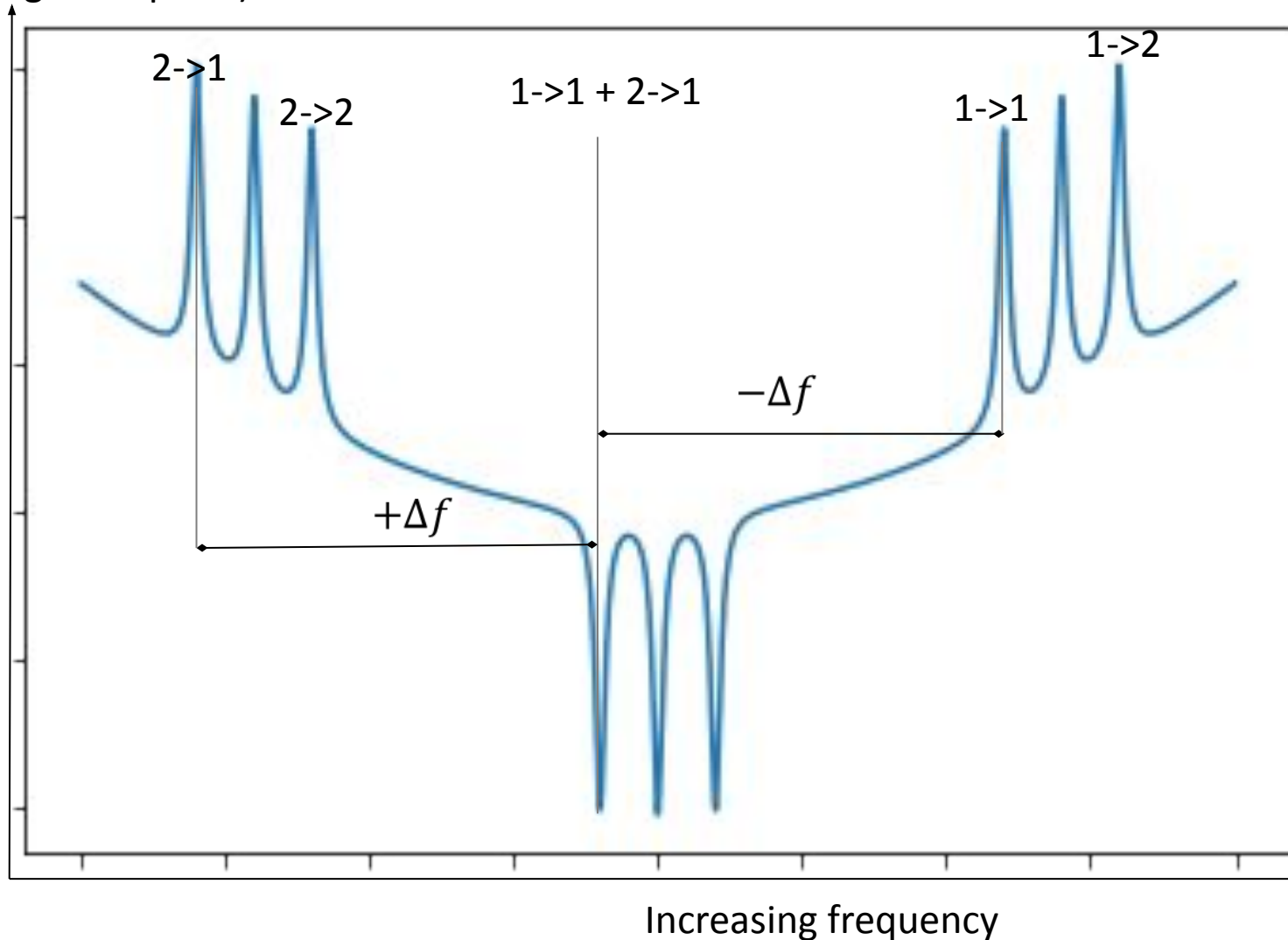


Because the two Doppler crossed frequencies start from different hyperfine ground states the pump does not steal from the probe.

Instead, the pump beam states randomly decay towards the opposing hyperfine, increasing the population the probe sees.

# Enhanced absorption

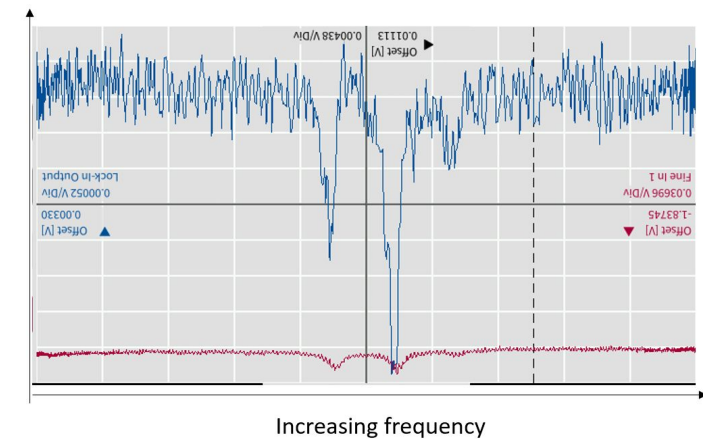
Increasing power  
(decreasing absorption)



Atoms moving towards the probe beam absorb the pump beam in the  $1 \rightarrow 1$  transition, which randomly decays, populating the  $F=2$  ground state for the probe beam which is absorbed in the  $2 \rightarrow 1$  transition.

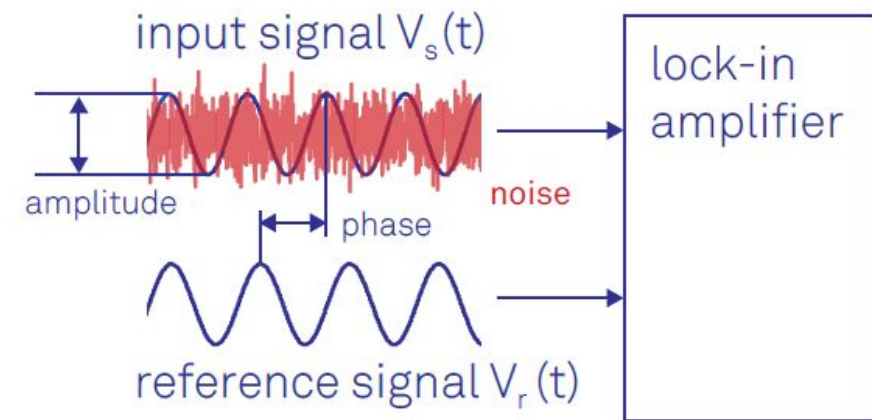
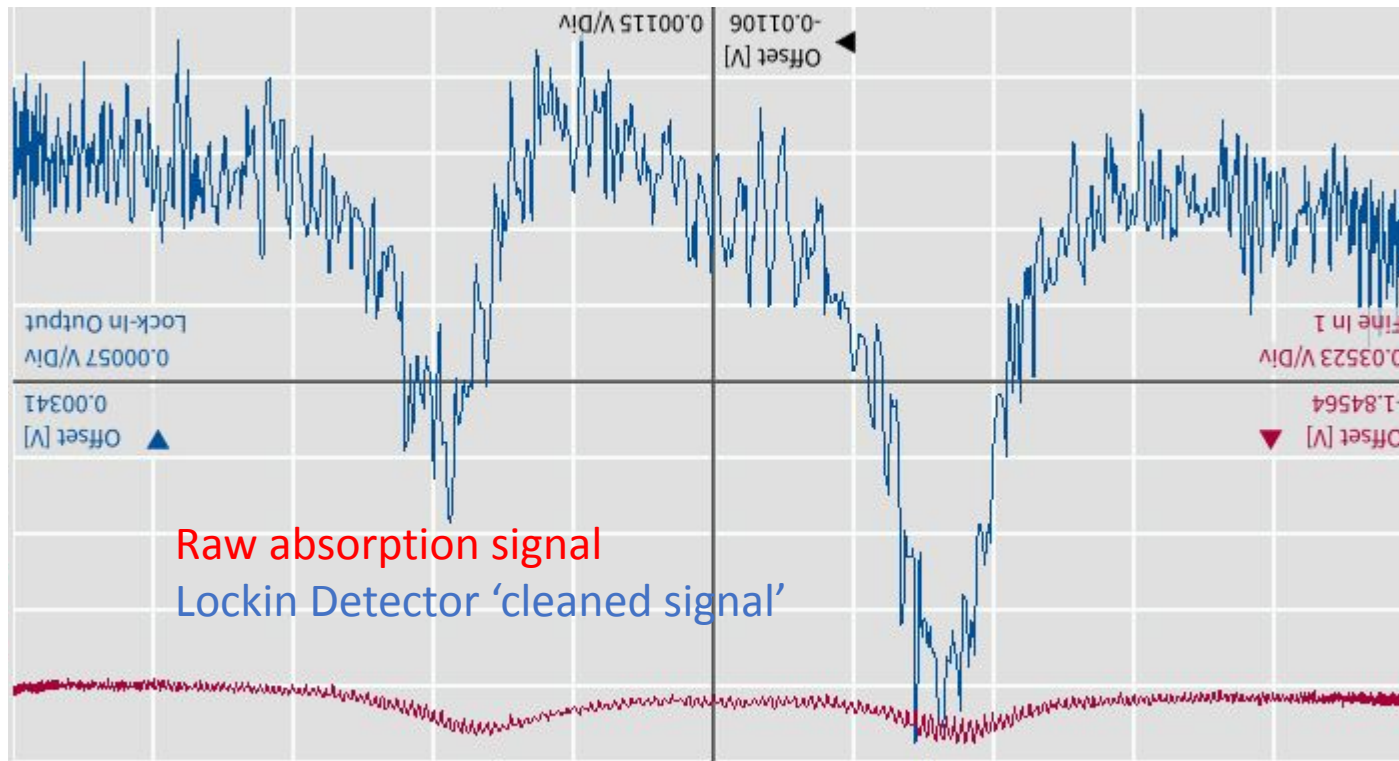
Atoms moving away from the probe beam absorb the pump beam in the  $2 \rightarrow 1$  transition, which randomly decays, populating the  $F=1$  ground state for the probe beam which is absorbed in the  $1 \rightarrow 2$  transition.

Increasing power  
(decreasing absorption)



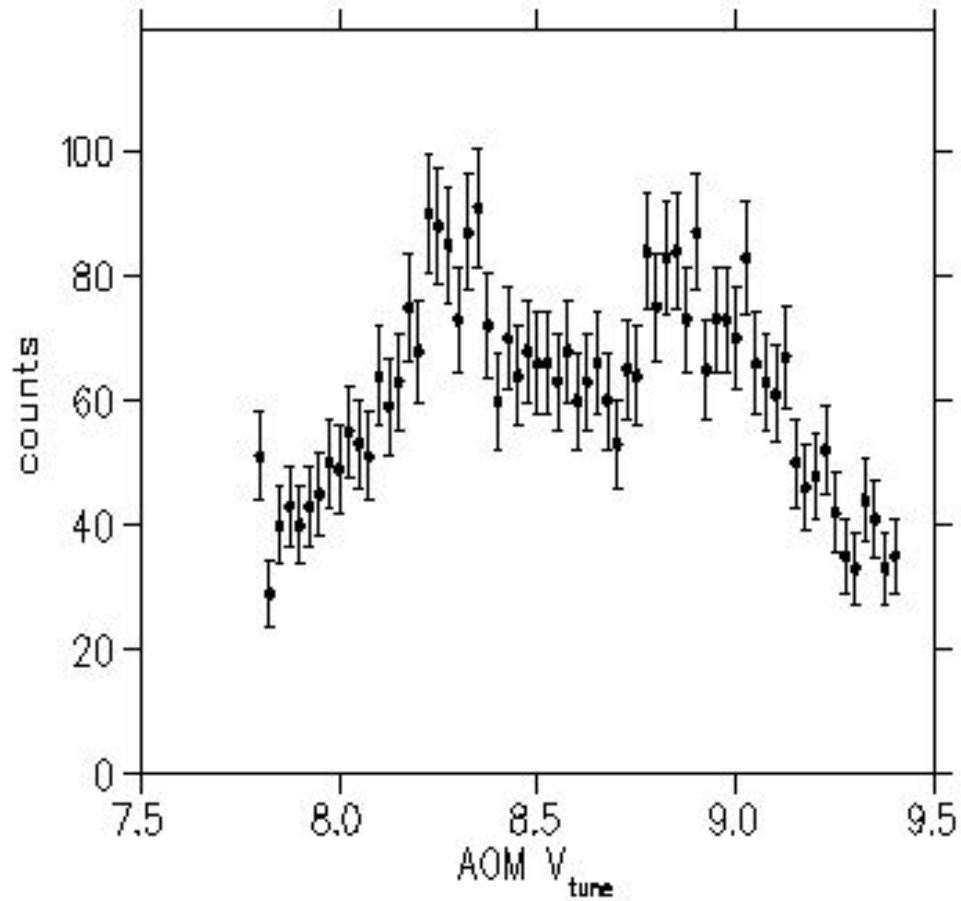
# Locking the laser frequency using absorption peaks

Using a solenoid and the Zeeman effect to produce slight high-frequency energy oscillations in the cell, correlating absorption peaks to our magnetic scan we can produce a cleaner signal and lock to the peak with a Proportional Integral Derivative control loop.

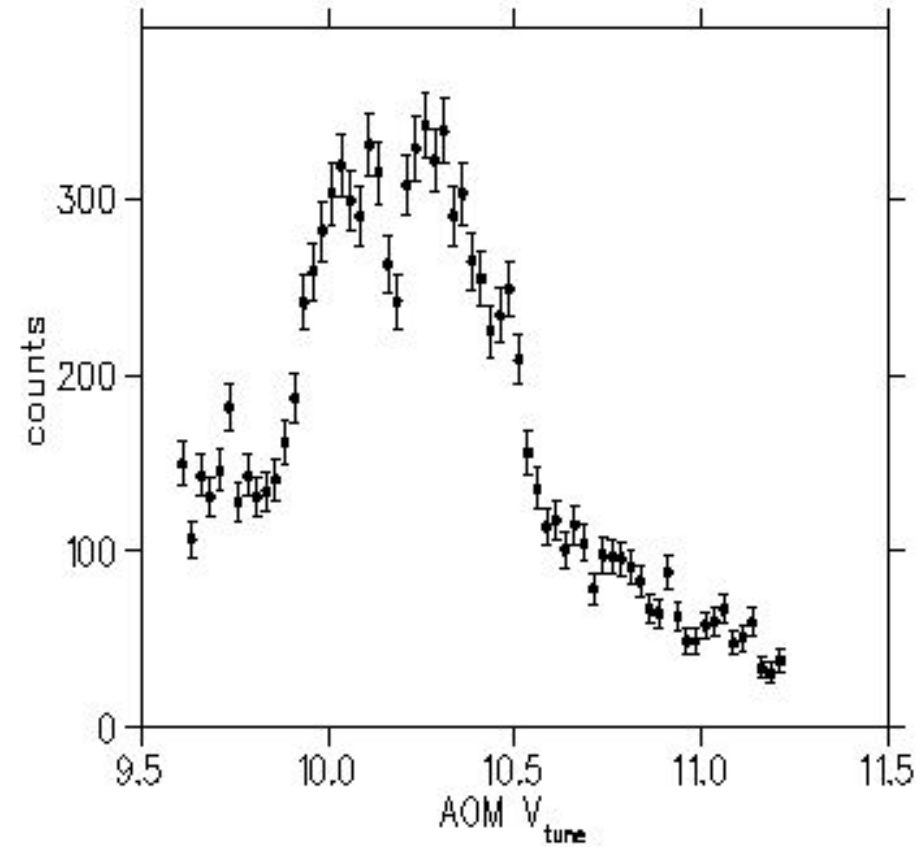


# Very early data

K41 2->1 and 2->2 absorptions



K41 1->1 and 1->2 absorptions



# Thank you!

